

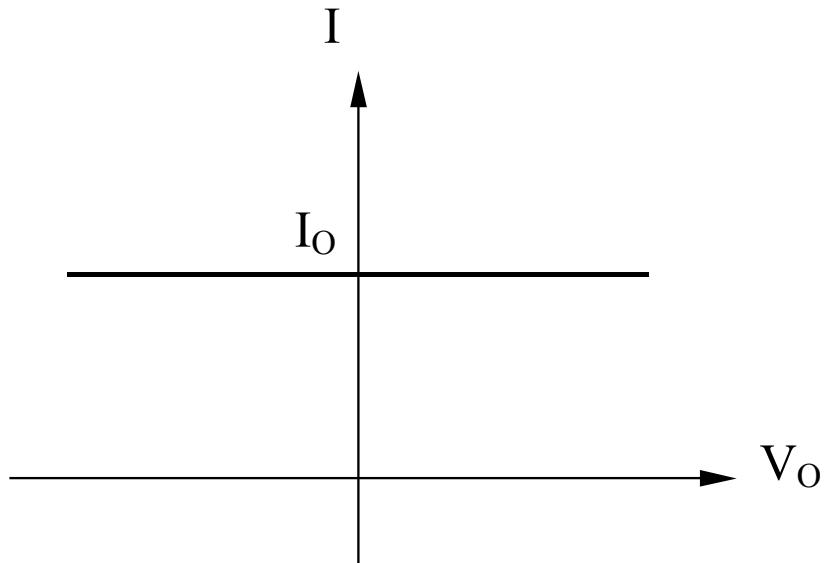
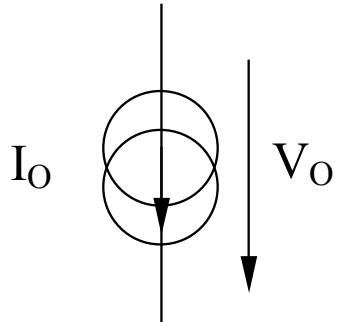
Capitolul 3

Surse de curent si surse de tensiune

3.1. Surse de curent

3.1. Surse de curent

3.1.1. Introducere



Parametri:

- Curentul de ieșire I_O [A]
- Rezistența de ieșire [Ω]

$$R_O = \left. \frac{dV_O}{dI_O} \right|_{V_{CC}, T=ct.}$$

- Tensiunea minima de iesire [V]
- Coeficientul de temperatura [A/K]

$$TC_{I_O} = \left. \frac{dI_O}{dT} \right|_{R_L, V_{CC} = ct.}$$

- Coeficientul relativ de temperatura [1/K]

$$RTC_{I_O} = \left. \frac{1}{I_O} \frac{dI_O}{dT} \right|_{R_L, V_{CC} = ct.}$$

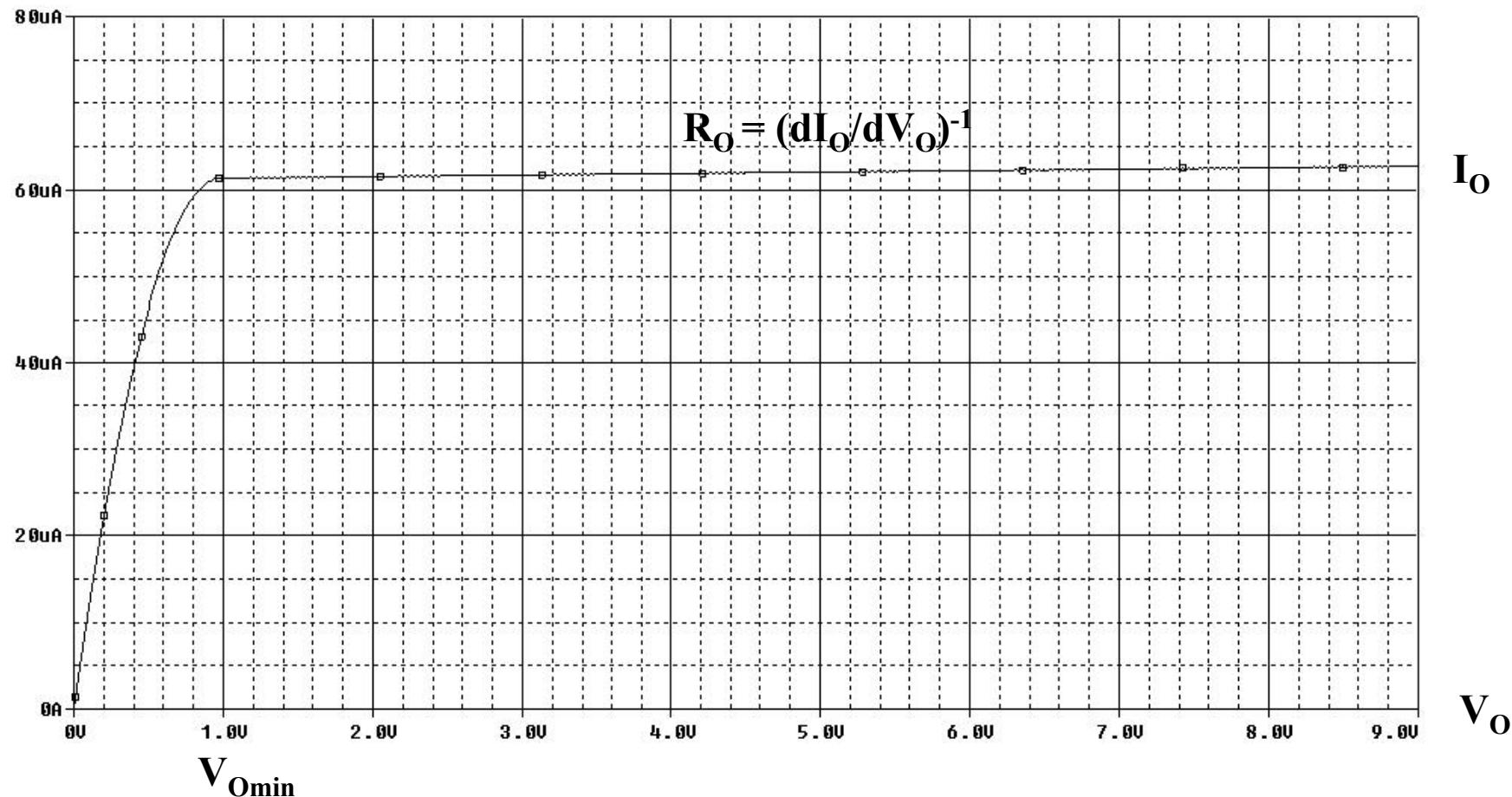
- Factorul de rejectie al tensiunii de alimentare (Power Supply Rejection Ratio) [A/V]

$$PSRR = \left. \frac{dI_O}{dV_{CC}} \right|_{R_L, T = ct.}$$

- Sensibilitatea curentului de iesire in raport cu variatiile tensiunii de alimentare [-]

$$S_{V_{CC}}^{I_O} = \left. \frac{dI_O / I_O}{dV_{CC} / V_{CC}} \right|_{R_L, T = ct.} = \left. \frac{V_{CC}}{I_O} \frac{dI_O}{dV_{CC}} \right|_{R_L, T = ct.}$$

I_O



Caracteristica de iesire a unei surse de curent

Clasificare

I. Surse de curent elementare

- complexitate redusa
- performante modeste

II. Surse de curent cascod

- rezistenta de iesire mare
- tensiune minima de iesire mare
- tensiune minima de alimentare mare

III. Surse de curent cu autopolarizare

- dependenta redusa I_O (V_{CC})
- necesita circuit de pornire

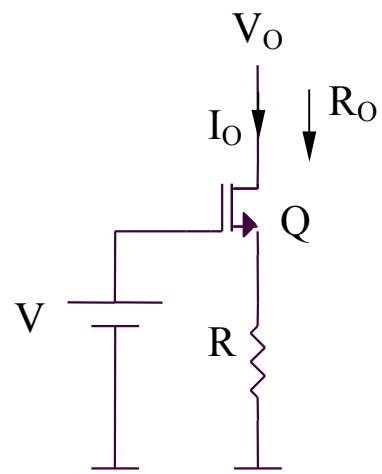
IV. Surse de curent compensate cu temperatura

- dependenta redusa de temperatura
- complexitate ridicata

3.1.2. Surse de curent elementare

3.1.2. Surse de curent elementare

Sursa de curent CMOS cu un tranzistor

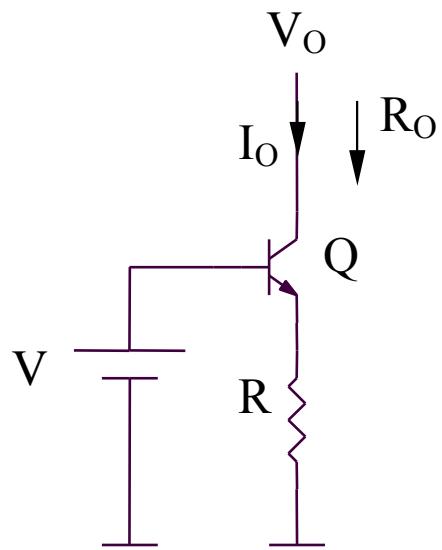


$$\left. \begin{array}{l} V = V_{GS} + I_O R \\ I_O = \frac{K}{2} (V_{GS} - V_T)^2 \end{array} \right\} \Rightarrow V = V_{GS} + \frac{KR}{2} (V_{GS} - V_T)^2$$
$$\Rightarrow V_{GS} (> V_T) \Rightarrow I_O$$

$$R_O = r_{ds} (1 + g_m R)$$

$$V_{O\min} = V - V_{GS} + (V_{GS} - V_T) = V - V_T$$

Sursa de curent bipolară cu un tranzistor

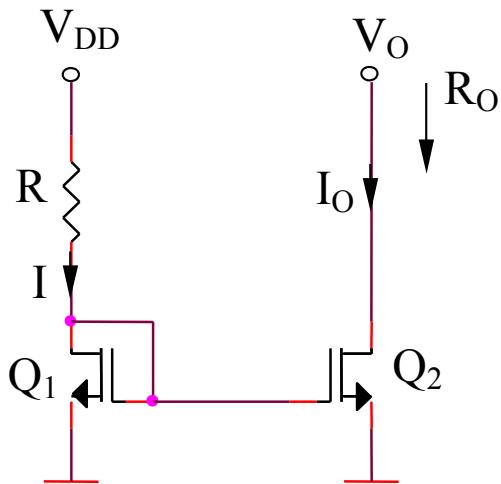


$$I_O = \frac{V - V_{BE}}{R}$$

$$R_O = r_o \left(1 + \frac{\beta R}{r_\pi + R} \right)$$

$$V_{O\min} = V - V_{BE} + V_{CEsat}$$

Oglinda de curent CMOS



Curentul de ieșire

$$\left. \begin{array}{l} V_{DD} = I_O R + V_{GS1} \\ I_O = \frac{K}{2} (V_{GS1} - V_T)^2 \end{array} \right\} \Rightarrow V_{DD} = \frac{KR}{2} (V_{GS1} - V_T)^2 + V_{GS1} \Rightarrow$$
$$\Rightarrow (V_{GS1})_{1,2} = V_T - \frac{1}{KR} \pm \frac{1}{KR} \sqrt{1 + 2KR(V_{DD} - V_T)}$$

V_{GS} trebuie sa fie mai mare decat V_T :

$$V_{GS1} = V_T - \frac{I}{KR} + \frac{I}{KR} \sqrt{1 + 2KR(V_{DD} - V_T)}$$

$$\Rightarrow I_O = \frac{1}{KR^2} [1 + KR(V_{DD} - V_T) - \sqrt{1 + 2KR(V_{DD} - V_T)}]$$

Rezistenta de iesire

$$R_O = r_{ds2} = \frac{1}{\lambda I_O}$$

Tensiunea minima de iesire

$$V_{O\min} = V_{DS2sat} = V_{GS2} - V_T = \sqrt{\frac{2I_O}{K}}$$

Efectul de modulare a lungimii canalului

$$\frac{I_O}{I} = \frac{\frac{K}{2}(V_{GS2} - V_T)^2(1 + \lambda V_{DS2})}{\frac{K}{2}(V_{GS1} - V_T)^2(1 + \lambda V_{DS1})} = \frac{1 + \lambda V_{DS2}}{1 + \lambda V_{DS1}} = \frac{1 + \lambda V_O}{1 + \lambda V_{GS1}}$$

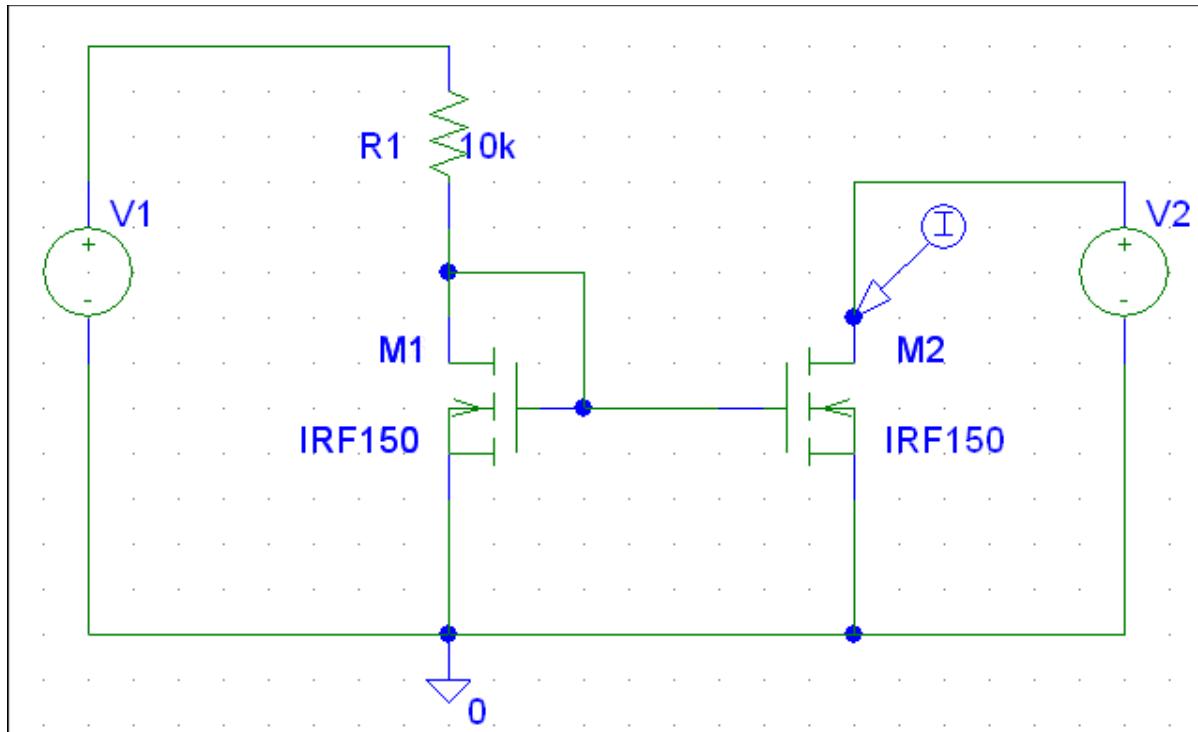
SIMULARI pentru oglinda de curent CMOS

Caracteristica de iesire

SIMULARI pentru oglinda de curent CMOS

Caracteristica de ieșire

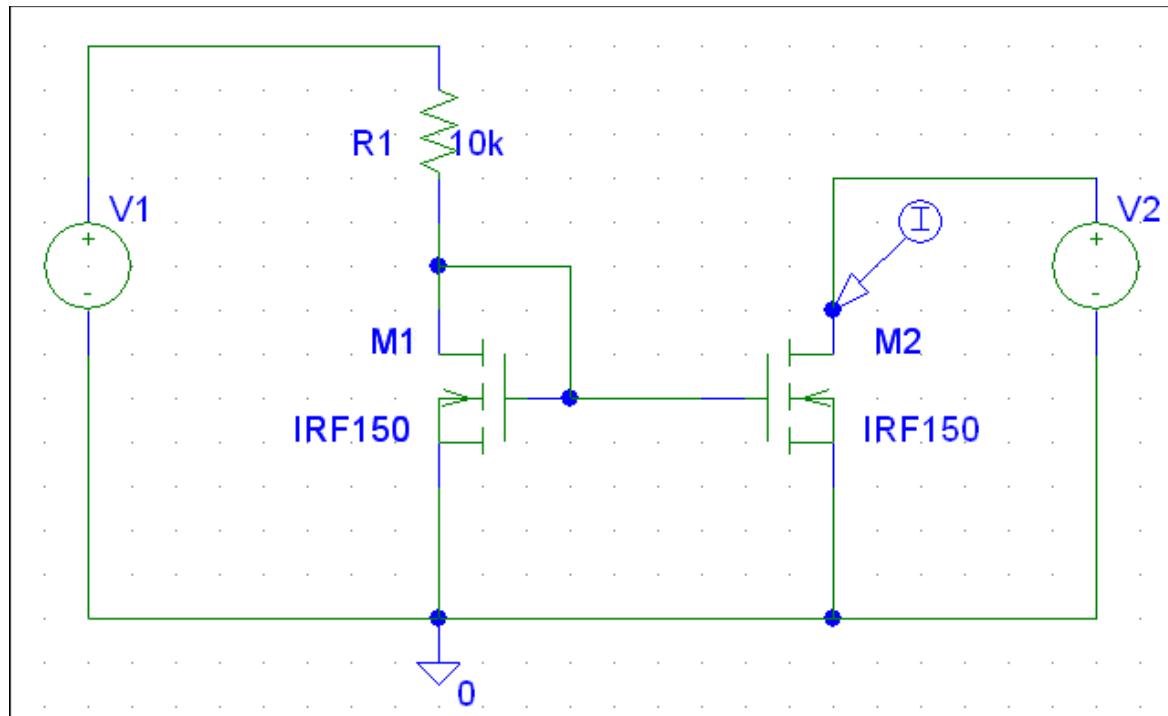
SIM 3.1: I_{D2} (V_2)



SIMULARI pentru oglinda de curent CMOS

Caracteristica de ieșire

SIM 3.2: I_{D2} (V_2), r_{ds2} - parametru

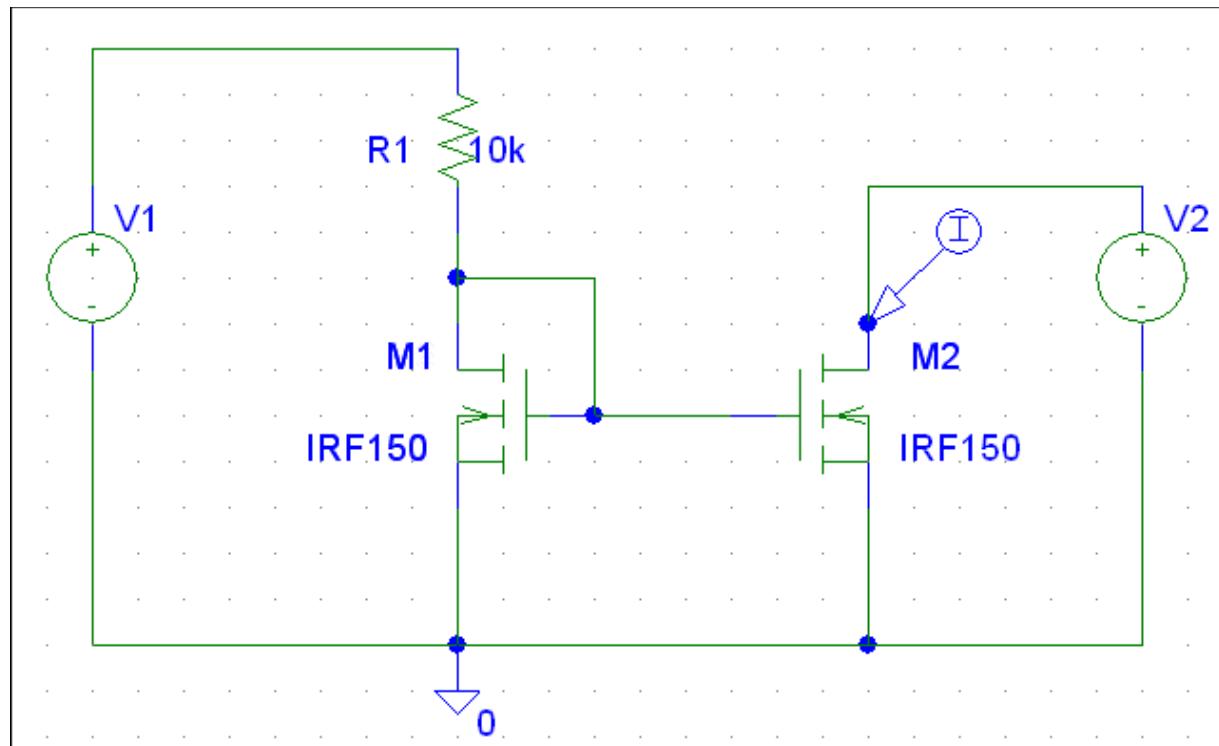


SIMULARI pentru oglinda de curent CMOS
Dependenta curentului de iesire de tensiunea de alimentare

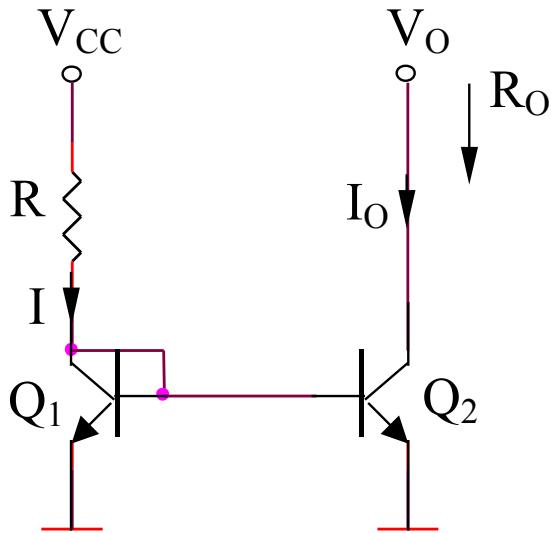
SIMULARI pentru oglinda de curent CMOS

Dependenta curentului de iesire de tensiunea de alimentare

SIM 3.3: I_{D2} ($V1$)



Oglinda de curent bipolară



Curent de ieșire

$$\left. \begin{array}{l} I = \frac{V_{CC} - V_{BE}}{R} \cong I_{S1} \exp\left(\frac{V_{BE1}}{V_{th}}\right) \\ I_O \cong I_{S2} \exp\left(\frac{V_{BE2}}{V_{th}}\right) \\ V_{BE1} = V_{BE2} \end{array} \right\} \Rightarrow \frac{I_O}{I} \cong \frac{I_{S2}}{I_{S1}} \Rightarrow I_O \cong \frac{V_{CC} - V_{BE}}{R} \frac{I_{S2}}{I_{S1}}$$

Rezistenta de iesire

$$R_O = r_o = \frac{V_A}{I_{C2}} = \frac{V_A}{I_O}$$

Tensiune minima de iesire

$$V_{O\min} = V_{CE2sat.}$$

Efect Early

$$I = \frac{V_{CC} - V_{BE}}{R} = I_{S1} \exp\left(\frac{V_{BE1}}{V_{th}}\right) \left(1 + \frac{V_{CE1}}{V_A}\right)$$

$$I_O = I_{S2} \exp\left(\frac{V_{BE2}}{V_{th}}\right) \left(1 + \frac{V_{CE2}}{V_A}\right)$$

$$\frac{I_O}{I} = \frac{I_{S2}}{I_{S1}} \frac{1 + \frac{V_{CE1}}{V_A}}{1 + \frac{V_{CE2}}{V_A}} = \frac{I_{S2}}{I_{S1}} \frac{1 + \frac{V_{BE1}}{V_A}}{1 + \frac{V_O}{V_A}}$$

Influenta β

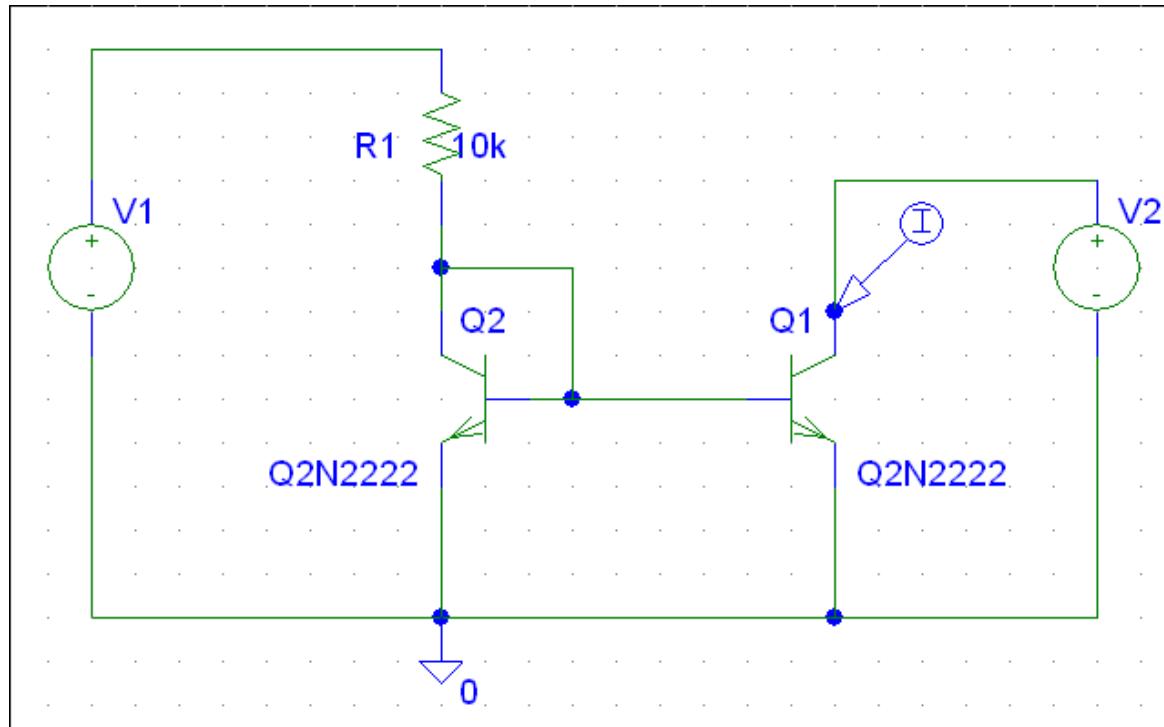
$$\frac{I_O}{I} = \frac{\beta I_B}{\beta I_B + 2I_B} = \frac{\beta}{\beta + 2}$$

SIMULARI pentru oglinda de curent bipolară
Caracteristica de ieșire

SIMULARI pentru oglinda de curent bipolară

Caracteristica de ieșire

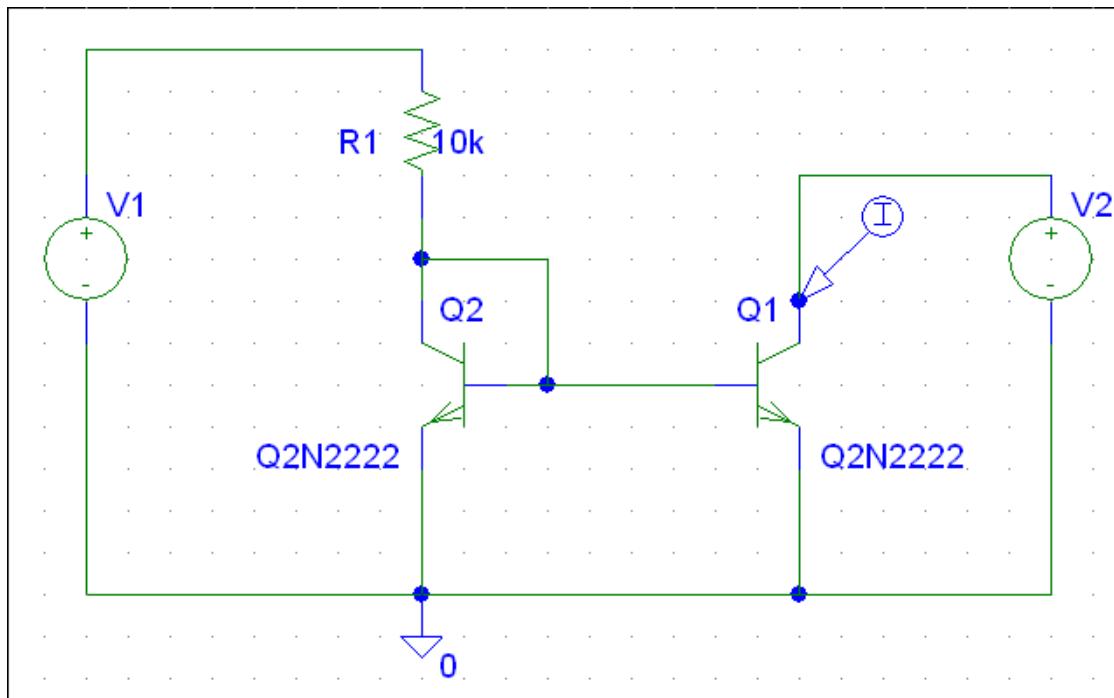
SIM 3.4: I_{C1} (V_2)



SIMULARI pentru oglinda de curent bipolară

Caracteristica de ieșire

SIM 3.5: $I_{C1}(V_2)$, V_{A1} - parametru

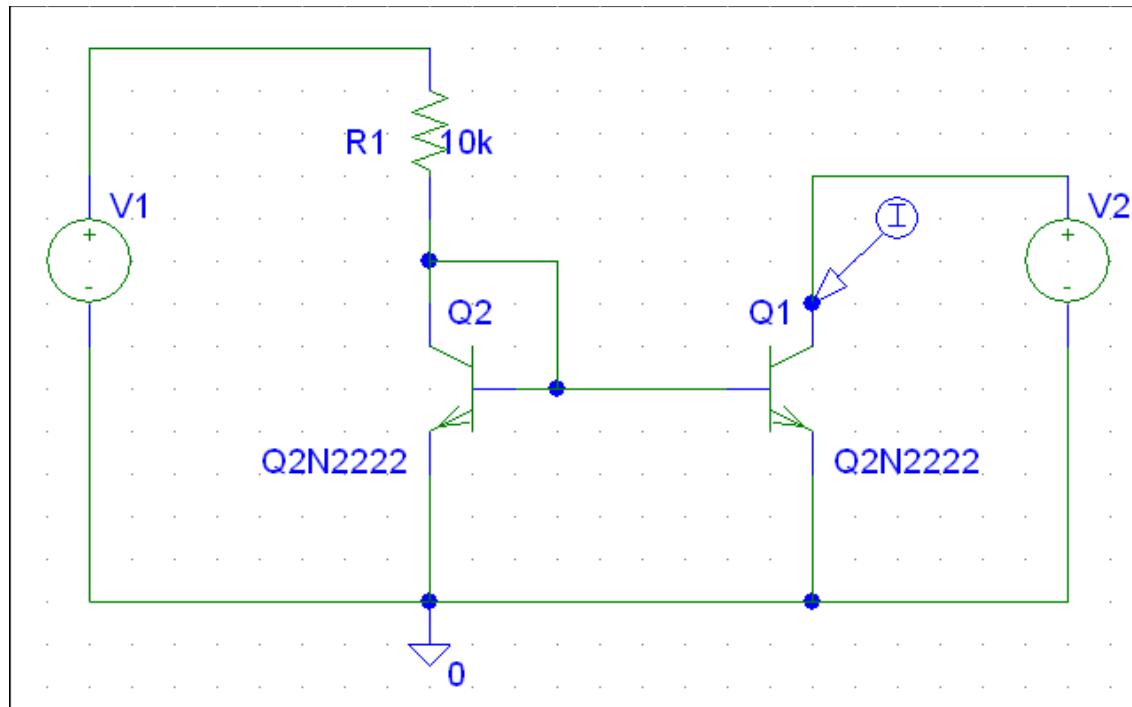


SIMULARI pentru oglinda de curent bipolară
Dependenta curentului de ieșire de tensiunea de alimentare

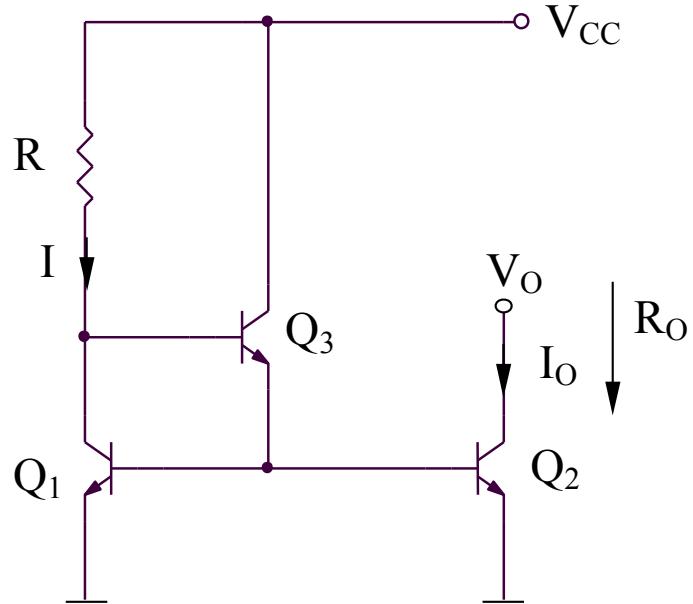
SIMULARI pentru oglinda de curent bipolară

Dependenta curentului de iesire de tensiunea de alimentare

SIM 3.6: I_{C1} (V_1)



Sursa de curent cu reducerea efectului β (1)



Curent de iesire

$$I_O \cong I = \frac{V_{CC} - 2V_{BE}}{R}$$

Rezistenta de iesire

$$R_O = r_o = \frac{V_A}{I_{C2}} = \frac{V_A}{I_O}$$

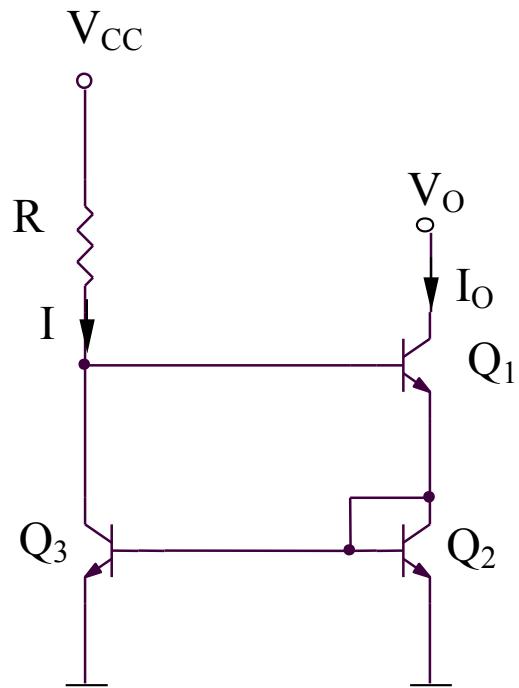
Tensiune minima de iesire

$$V_{O\min} = V_{CE2sat.}$$

Influenta β

$$\frac{I_O}{I} = \frac{\beta I_B}{\beta I_B + \frac{2I_B}{\beta + 1}} = \frac{1}{1 + \frac{2}{\beta^2 + \beta}} \cong 1$$

Sursa de curent cu reducerea efectului β (2)



Curent de ieșire

$$I_O \cong I = \frac{V_{CC} - 2V_{BE}}{R}$$

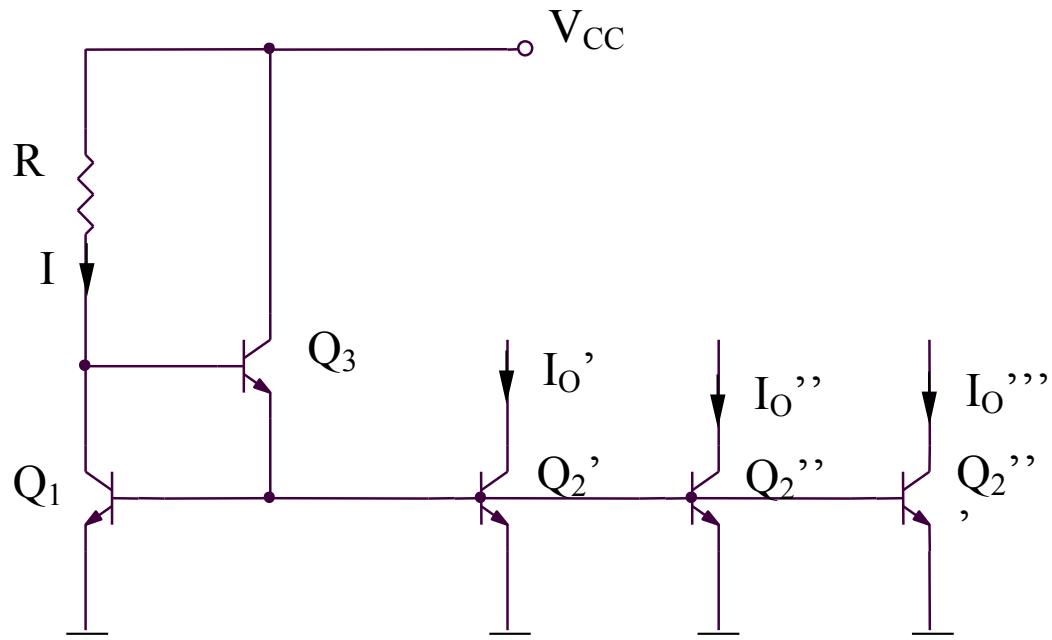
Tensiune minima de ieșire

$$V_{O\min} = V_{BE2} + V_{CE1sat.}$$

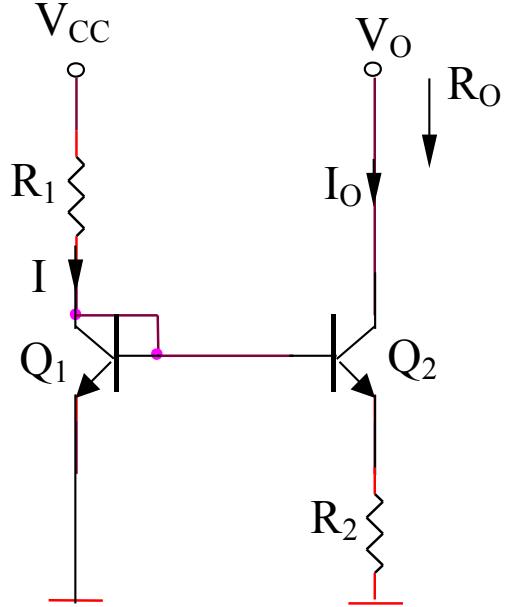
Influenta β

$$\frac{I_O}{I} = \frac{\frac{\beta(\beta+2)}{\beta+1} I_B}{\beta I_B + \frac{\beta+2}{\beta+1} I_B} = \frac{1}{1 + \frac{2}{\beta^2 + 2\beta}} \cong 1$$

Sursa de curent multipla



Sursa de curent Widlar bipolară



Curentul de ieșire

$$I = \frac{V_{CC} - V_{BE}}{R_1}$$

$$I_O = \frac{V_{BE1} - V_{BE2}}{R_2} = \frac{V_{th} \ln\left(\frac{I}{I_S}\right) - V_{th} \ln\left(\frac{I_O}{I_S}\right)}{R_2}$$

$$I_O = \frac{V_{th}}{R_2} \ln\left(\frac{I}{I_O}\right) = \frac{V_{th}}{R_2} \ln\left(\frac{V_{CC} - V_{BE}}{R_1 I_O}\right)$$

Tensiunea minima de ieșire

$$V_{O\min} = V_{CE2sat.} + I_O R_2$$

Rezistența de ieșire

$$R_O = r_o \left(1 + \frac{\beta R_2}{r_{\pi 2} + R_2 + (1/g_m 1) // R_1} \right) = \frac{V_A}{I_O} \left(1 + \frac{\beta R_2}{r_{\pi 2} + R_2 + (1/g_m 1) // R_1} \right)$$

PSRR

$$\frac{dI_O}{dV_{CC}} = \frac{d}{dV_{CC}} \left[\frac{V_{th}}{R_2} \ln \left(\frac{V_{CC} - V_{BE}}{R_1 I_O} \right) \right]$$

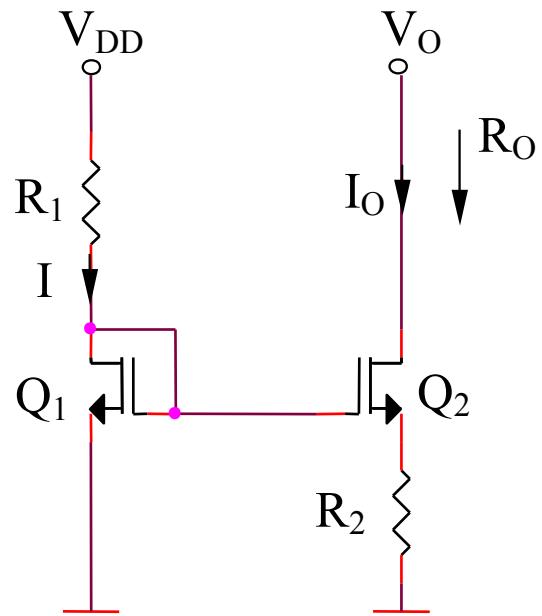
$$\frac{dI_O}{dV_{CC}} = \frac{V_{th}}{R_2} \frac{R_1 I_O - (V_{CC} - V_{BE}) R_1}{(R_1 I_O)^2} \frac{\frac{dI_O}{dV_{CC}}}{R_1}$$

$$\frac{dI_O}{dV_{CC}} = \frac{\frac{1}{R_2} \frac{V_{th}}{V_{CC} - V_{BE}}}{1 + \frac{V_{th}}{R_2 I_O}}$$

Sensibilitatea curentului de iesire in raport cu variatiile tensiunii de alimentare

$$S_{V_{CC}}^{I_O} = \frac{V_{CC}}{I_O} \frac{dI_O}{dV_{CC}} = \frac{1}{1 + \frac{R_2 I_O}{V_{th}}} = \frac{1}{1 + \ln \left(\frac{V_{CC} - V_{BE}}{R_1 I_O} \right)}$$

Sursa de curent CMOS



Curentul de ieșire

$$V_{GS1} = V_T - \frac{1}{KR_1} + \frac{1}{KR_1} \sqrt{1 + 2KR_1(V_{DD} - V_T)}$$

$$V_{GS1} = V_{GS2} + I_O R_2 = V_{GS2} + \frac{KR_2}{2} (V_{GS2} - V_T)^2$$

$$(V_{GS2} > V_T)$$

$$I_O = \frac{K}{2} (V_{GS2} - V_T)^2 (1 + \lambda V_{DS2})$$

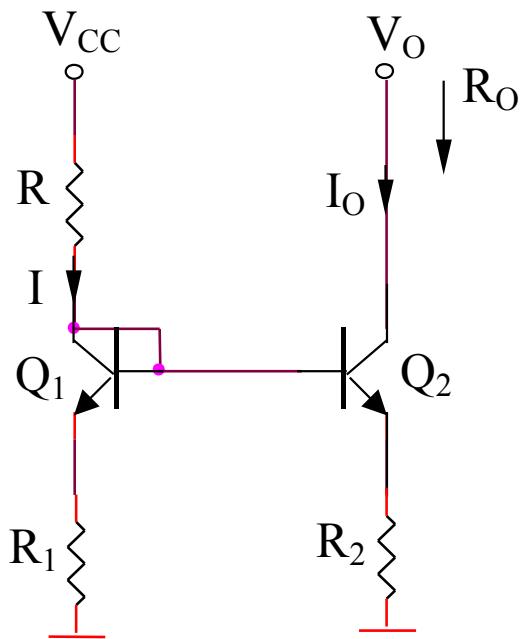
Tensiunea minima de ieșire

$$V_{O\min} = V_{DS2sat} + I_O R_2 = \sqrt{\frac{2I_O}{K}} + I_O R_2$$

Rezistența de ieșire

$$R_O = r_{ds2} (1 + g_m R_2)$$

Sursa de curent standard



Rezistenta de iesire

$$R_O = r_{o2} \left(1 + \frac{\beta R_2}{R_2 + r_{\pi2} + R // (1/g_m1 + R_1)} \right)$$

Curentul de iesire

$$v_{BE1} + R_1 I = v_{BE2} + R_2 I_O$$

$$I_O = \frac{1}{R_2} (R_1 I + v_{BE1} - v_{BE2})$$

$$\frac{I_O}{I} = \frac{R_1}{R_2} + \frac{V_{th}}{R_2 I} \ln \left(\frac{I}{I_O} \frac{I_{S2}}{I_{S1}} \right)$$

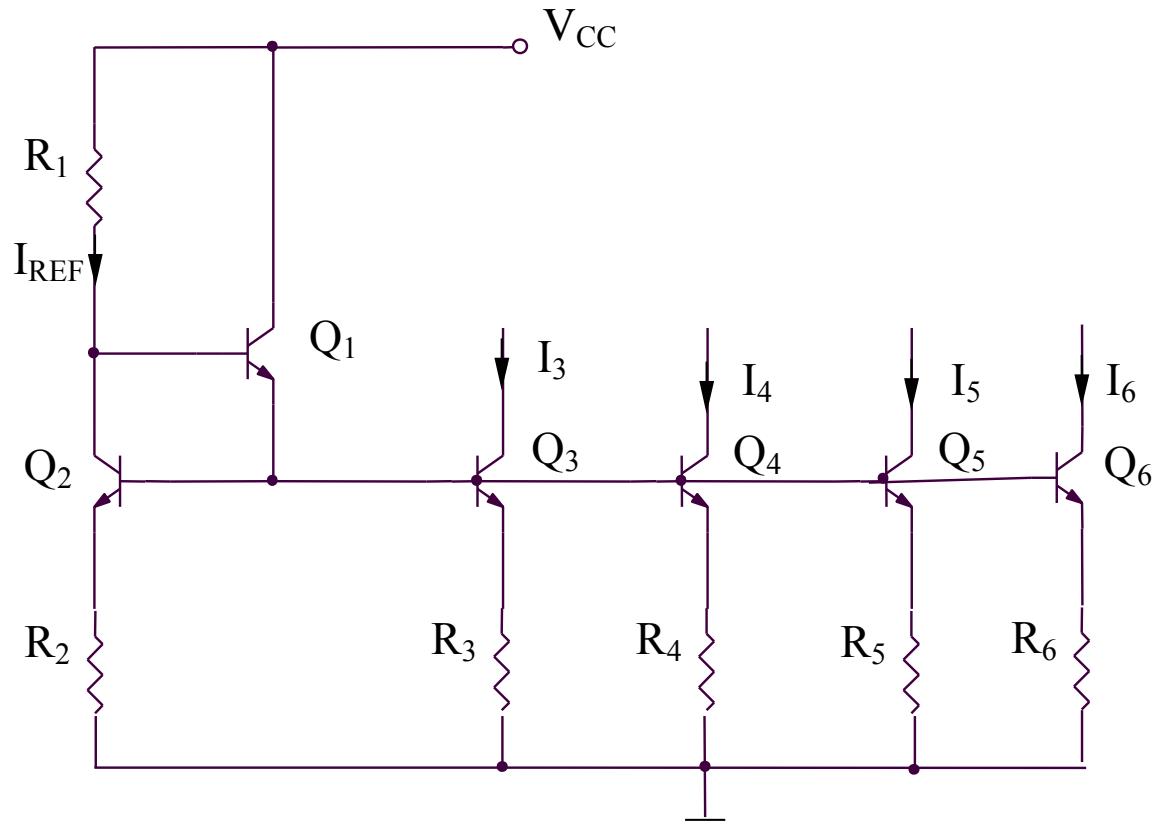
Se poate determina I/I_O deoarece:

$$I = \frac{V_{CC} - v_{BE}}{R + R_1}$$

Daca $R_1 I \gg v_{BE1} - v_{BE2}$:

$$\frac{I_O}{I} = \frac{R_1}{R_2}$$

Sursa de curent standard cu iesire multipla



Daca ariile tranzistoarelor sunt alese in asa fel incat densitatile de curent sa fie egale, atunci tensiunile baza-emitor vor fi egale.

$$v_{BE2} - v_{BE3} = V_{th} \ln \left(\frac{I_{REF}}{I_3} \frac{I_{S3}}{I_{S2}} \right) = V_{th} \ln \left(\frac{jA_2}{jA_3} \frac{A_3}{A_2} \right) = 0$$

Deci:

$$v_{BE2} = \dots = v_{BE6}$$

si:

$$I_3 R_3 = I_4 R_4 = I_5 R_5 = I_6 R_6 = I_{REF} R_2$$

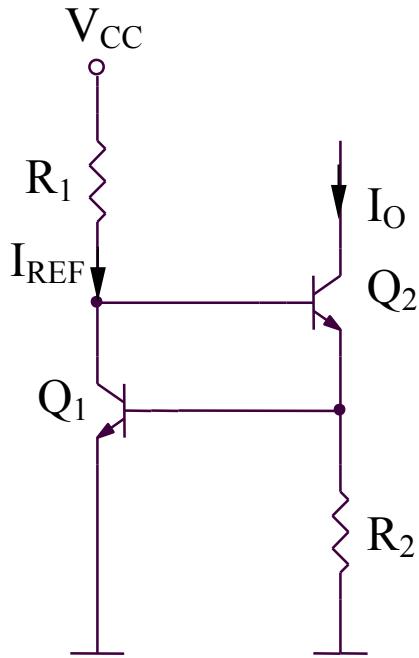
Cei patru curenti de iesire au expresiile:

$$I_3 = I_{REF} \frac{R_2}{R_3}; \dots; I_6 = I_{REF} \frac{R_2}{R_6}$$

unde:

$$I_{REF} = \frac{V_{CC} - 2v_{BE}}{R_1 + R_2}$$

Sursa de curent utilizand ca referinta tensiunea baza-emitor



$$I_O = \frac{v_{BE1}}{R_2} = \frac{V_{th}}{R_2} \ln \frac{V_{CC} - 2v_{BE}}{R_1 I_S}$$

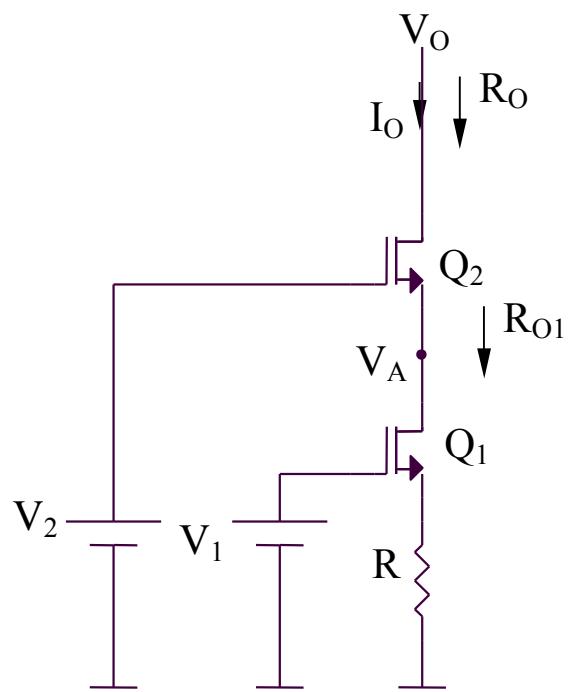
3.1.3. Surse de curent cascod

3.1.3. Surse de curent cascod

Sursa de curent cascod CMOS (1)

Curentul de iesire

$$\left. \begin{array}{l} V_1 = V_{GS1} + I_O R \\ I_O = \frac{K}{2} (V_{GS1} - V_T)^2 \end{array} \right\} \Rightarrow V_1 = V_{GS1} + \frac{KR}{2} (V_{GS1} - V_T)^2 \Rightarrow V_{GS1} (> V_T) \Rightarrow I_O$$



Rezistenta de iesire

$$R_O = r_{ds2} (1 + g_m R_{O1}) \approx g_m^2 r_{ds2}^2 R$$

$$R_{O1} = r_{ds1} (1 + g_m R)$$

Tensiunea minima de iesire

$$V_{Omin} = V_2 - V_{GS2} + (V_{GS1} - V_T) = V_2 - V_T$$

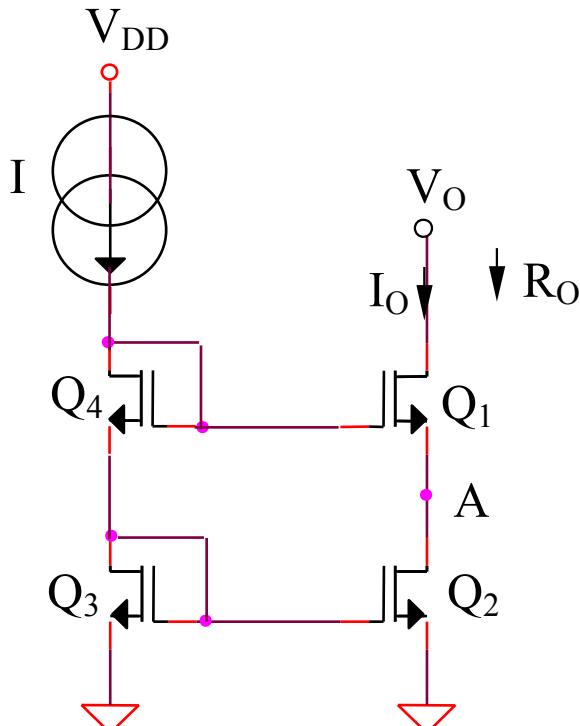
Este necesar ca:

$$V_{DS1} > V_{DS1sat} \Leftrightarrow$$

$$\Leftrightarrow (V_2 - V_{GS2}) - (V_1 - V_{GS1}) > V_{DS1sat} \Leftrightarrow$$

$$\Leftrightarrow V_2 - V_1 > V_{DS1sat} = V_{GS} - V_T = \sqrt{\frac{2I_O}{K}}$$

Oglinda de curent cascod CMOS (2)



Curentul de iesire

$$\frac{I_O}{I} = \frac{1 + \lambda V_{DS2}}{1 + \lambda V_{DS3}}$$

Rezistenta de iesire

$$R_O = r_{ds1} \left(1 + g_m r_{ds2} \right) \cong g_m r_{ds}^2$$

Tensiunea minima de iesire

$$V_{O\min} = V_A + V_{DS1sat} = V_{GS} + (V_{GS} - V_T)$$

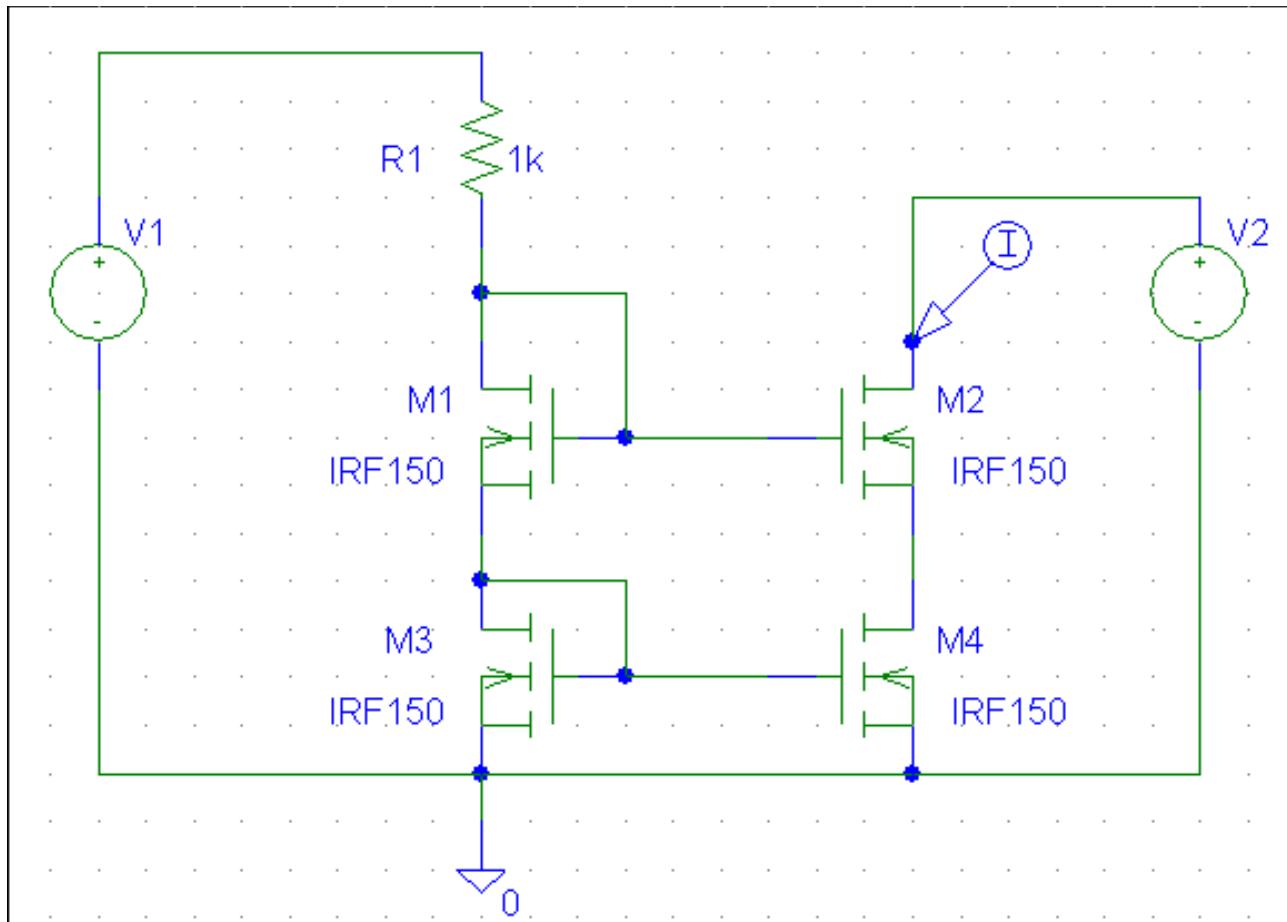
$$V_{O\min} = 2V_{GS} - V_T \cong V_T + 2\sqrt{\frac{2I}{K}}$$

SIMULARI pentru oglinda de curent CMOS cascod
Caracteristica de iesire

SIMULARI pentru oglinda de curent CMOS cascod

Caracteristica de iesire

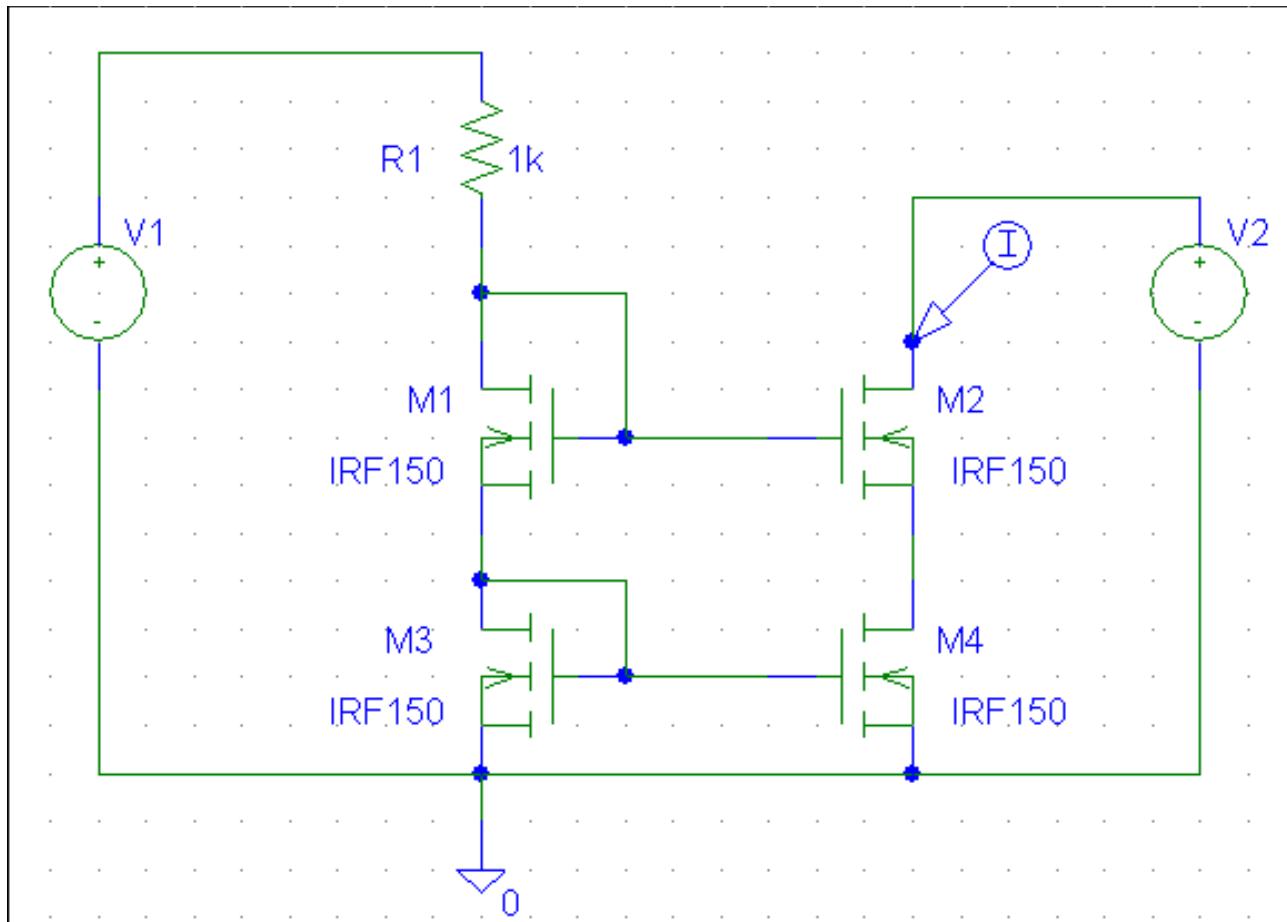
SIM 3.7: I_{D2} (V_2)



SIMULARI pentru oglinda de curent CMOS cascod

Caracteristica de iesire

SIM 3.8: I_{D2} (V_2), r_{ds2} , r_{ds4} - parametri

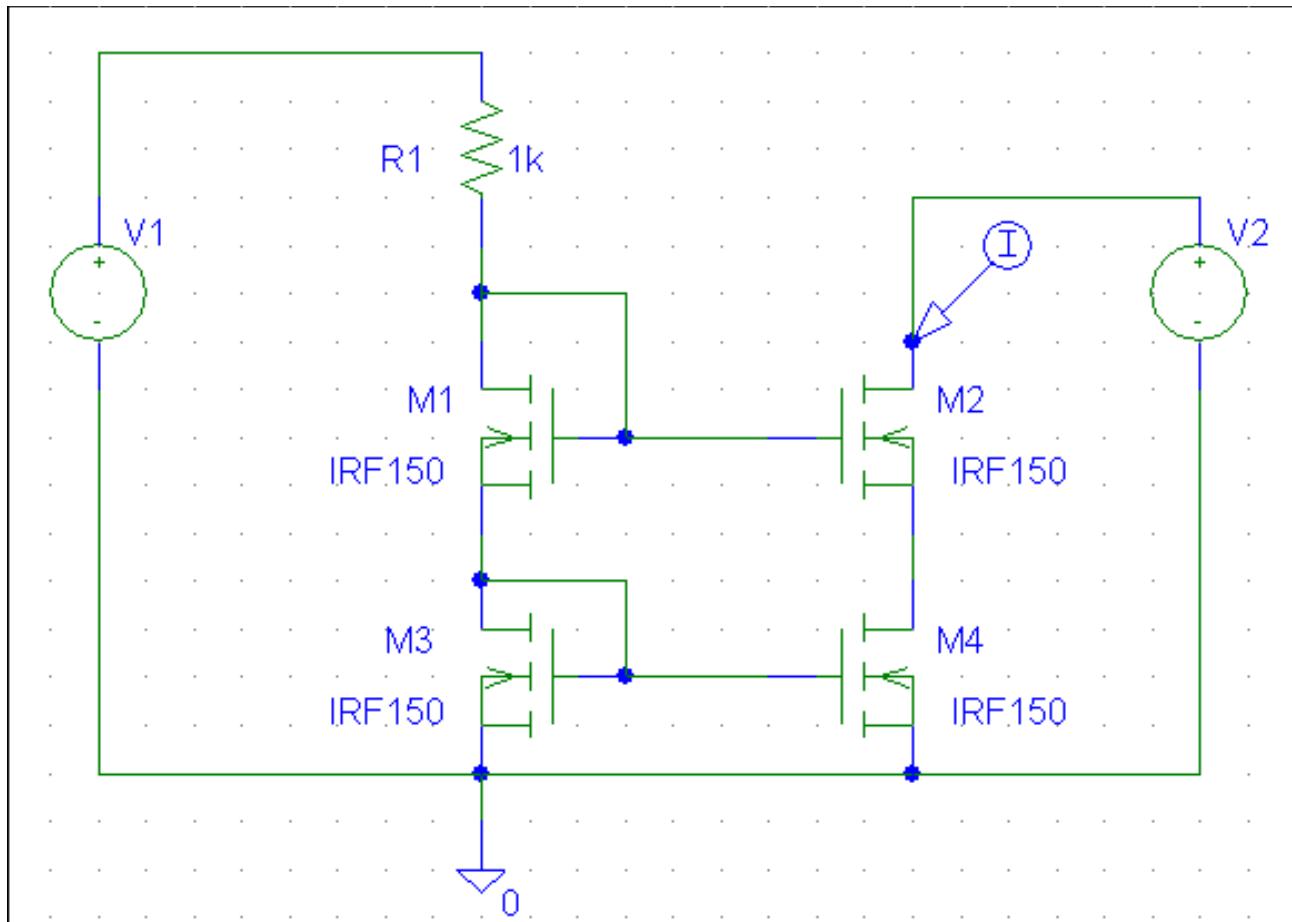


SIMULARI pentru oglinda de curent CMOS cascod
Dependenta curentului de iesire de tensiunea de alimentare

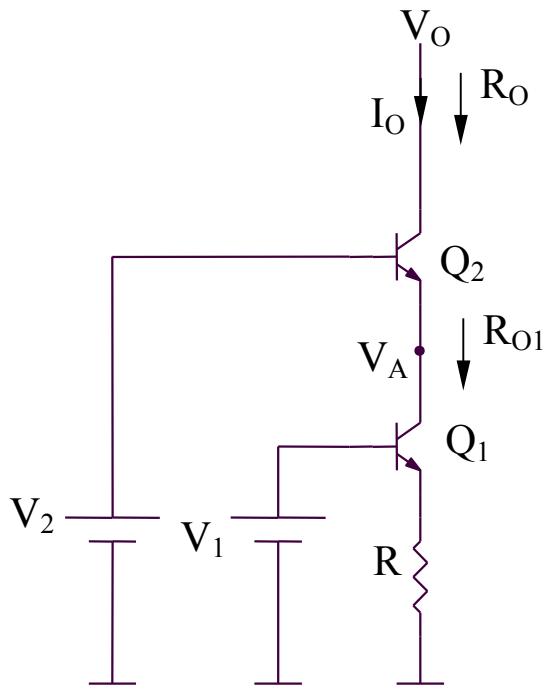
SIMULARI pentru oglinda de curent CMOS cascod

Dependenta curentului de iesire de tensiunea de alimentare

SIM 3.9: I_{D2} (V_1)



Sursa de curent cascod bipolară (1)



Curentul de ieșire

$$I_O = \frac{V_1 - V_{BE1}}{R}$$

Rezistența de ieșire

$$R_O = r_{o2} \left(1 + \frac{\beta R_{O1}}{r_{\pi2} + R_{O1}} \right) \cong \beta r_{O2}$$

$$R_{O1} = r_{o1} \left(1 + \frac{\beta R}{r_{\pi1} + R} \right) \gg r_{\pi2}$$

Tensiune minima de ieșire

$$V_{O\min} = V_A + V_{CE2sat} = V_2 - V_{BE2} + V_{CE2sat}$$

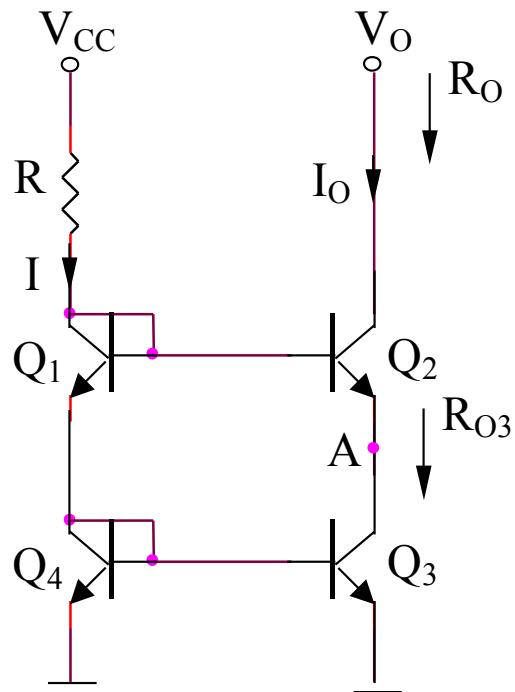
Este necesar ca:

$$V_{CE1} > V_{CE1sat} \Leftrightarrow$$

$$\Leftrightarrow (V_2 - V_{BE2}) - (V_1 - V_{BE1}) > V_{CE1sat} \Leftrightarrow$$

$$\Leftrightarrow V_2 - V_1 > V_{CE1sat}$$

Oglinda de curent cascod bipolară (2)



Curentul de ieșire

$$I_O = I = \frac{V_{CC} - 2v_{BE}}{R}$$

Rezistența de ieșire

$$R_O = r_{o2} \left(1 + \beta \frac{R_{O3}}{r_{\pi2} + R_{O3} + R/(2/g_m1)} \right)$$

$$R_{O3} = r_{o3} \gg r_{\pi2}, R/(2/g_m1)$$

Deci:

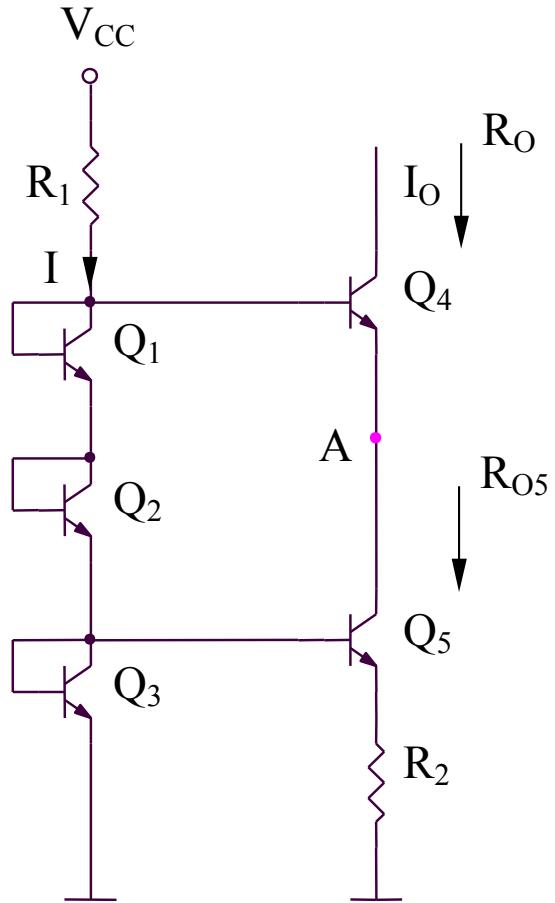
$$R_O \approx \beta r_{o2}$$

Tensiunea minima de ieșire

$$V_{O\min} = V_A + V_{CE2sat}$$

$$V_A = v_{BE1} + v_{BE4} - v_{BE2} = v_{BE}$$

Sursa de curent cascod bipolară (3)



Curentul de ieșire

$$I_O = \frac{v_{BE3} - v_{BE5}}{R_2} = \frac{V_{th}}{R_2} \ln\left(\frac{I}{I_O}\right)$$

$$I = \frac{V_{CC} - 3v_{BE}}{R_1}$$

Rezistența de ieșire

$$R_O = r_{o4} \left(1 + \beta \frac{R_{O5}}{r_{\pi4} + R_{O5} + R_1 / (3/g_{m1})} \right)$$

$$R_{O5} \cong r_{o5} \left(1 + \frac{\beta R_2}{r_{\pi5} + R_2 + 1/g_{m3}} \right)$$

$$R_{O5} \gg r_{\pi4}, R_1 / (3/g_{m1})$$

Deci:

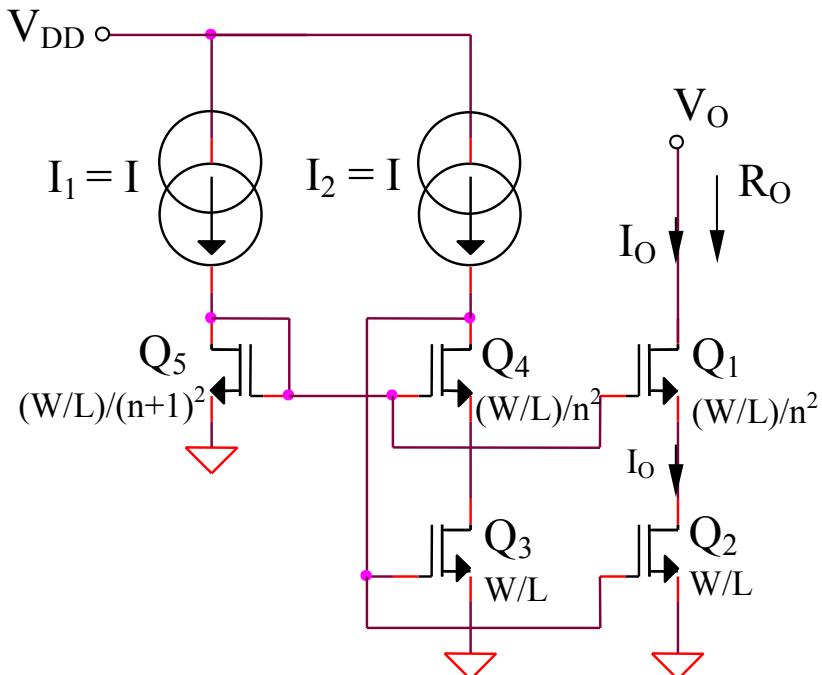
$$R_O \cong \beta r_{o4}$$

Tensiunea minima de ieșire

$$V_{O\min} = V_A + V_{CE4sat}$$

$$V_A = 2v_{BE}$$

Sursa de curent cascod MOS (3)



Curentul de ieșire

$$I_O = I$$

Rezistența de ieșire

$$R_O = r_{ds1} \left(1 + g_m r_{ds2} \right) \cong g_m r_{ds}^2$$

Tensiunea minima de ieșire

$$\left. \begin{aligned} I &= \frac{K'}{2} \frac{W / L}{(n + 1)^2} (V_{GS5} - V_T)^2 \\ I &= \frac{K'}{2} \frac{W / L}{n^2} (V_{GS1(4)} - V_T)^2 \\ I &= \frac{K'}{2} (W / L) (V_{GS2(3)} - V_T)^2 \end{aligned} \right\} \Rightarrow$$

$$\Rightarrow \begin{cases} V_{GS5} - V_T = (n+1)(V_{GS2(3)} - V_T) \\ V_{GS1(4)} - V_T = n(V_{GS2(3)} - V_T) \end{cases}$$

Tensiunea drena-sursa a tranzistorului Q₂ este:

$$V_{DS2} = V_{GS5} - V_{GS1} = (V_{GS5} - V_T) - (V_{GS1} - V_T) = V_{GS2} - V_T = V_{DS2sat}$$

Deci, Q₂ este polarizat la limita de saturatie. Rezulta:

$$V_{Omin} = V_{DS1sat} + V_{DS2} = (n+1)(V_{GS2} - V_T) = (n+1)\sqrt{\frac{2I}{K}}$$

3.1.4. Surse de curent cu autopolarizare

3.1.4. Surse de curent cu autopolarizare

Oglinda de curent

$$I_O = \frac{V_{CC} - v_{BE}}{R}$$

$$S_{V_{CC}}^{I_O} = \frac{V_{CC}}{I_O} \frac{\partial I_O}{\partial V_{CC}} \cong 1$$

Sursa de curent Widlar bipolară

$$I_O = \frac{V_{th}}{R_2} \ln \frac{I}{I_O}$$

$$\frac{\partial I_O}{\partial V_{CC}} = \frac{V_{th}}{R_2} \frac{I_O}{I} \left(\frac{1}{I_O} \frac{\partial I}{\partial V_{CC}} - \frac{I}{I_O^2} \frac{\partial I_O}{\partial V_{CC}} \right)$$

$$\frac{\partial I_O}{\partial V_{CC}} = \frac{\frac{V_{th}}{IR_2}}{1 + \frac{V_{th}}{R_2 I_O}} \frac{\partial I}{\partial V_{CC}}$$

$$S_{V_{CC}}^{I_O} = \frac{V_{CC}}{I_O} \frac{\partial I_O}{\partial V_{CC}} = \frac{V_{CC}}{I} \frac{1}{1 + \frac{R_2 I_O}{V_{th}}} \frac{\partial I}{\partial V_{CC}} \cong \frac{1}{1 + \frac{R_2 I_O}{V_{th}}}$$

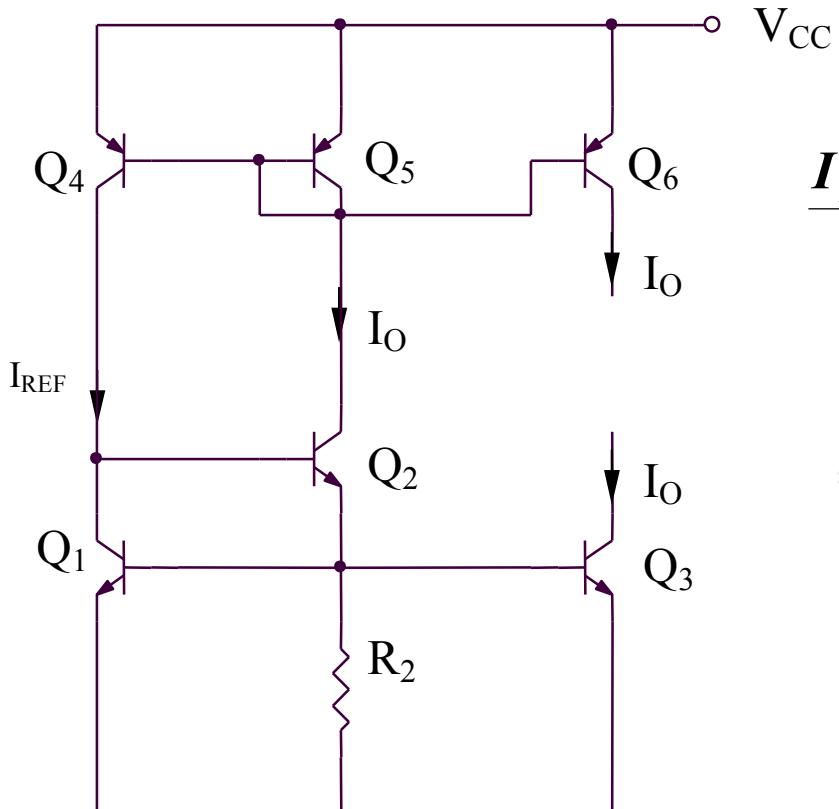
Sursa de curent utilizand ca referinta tensiunea baza-emitor

$$I_O = \frac{V_{th}}{R_2} \ln \frac{V_{CC} - 2v_{BE}}{R_1 I_S}$$

$$\frac{\partial I_O}{\partial V_{CC}} \cong \frac{V_{th}}{R_2} \frac{R_1 I_S}{V_{CC} - 2v_{BE}} \frac{1}{R_1 I_S}$$

$$S_{V_{CC}}^{I_O} \cong \frac{V_{th}}{v_{BE}} \cong 4\%$$

Sursa de curent cu autopolarizare utilizand ca referinta tensiunea baza-emitor



$$\left. \begin{aligned} I_O &= \frac{v_{BE1}}{R_2} = \frac{V_{th}}{R_2} \ln \frac{I_{REF}}{I_S} \\ \frac{I_{REF}}{I_O} &= \frac{1 + \frac{V_{CC} - 2v_{BE}}{V_A}}{1 + \frac{v_{BE}}{V_A}} \cong 1 + \frac{V_{CC} - 2v_{BE}}{V_A} \end{aligned} \right\} \Rightarrow I_O = \frac{V_{th}}{R_2} \ln \frac{I_O}{I_S} + \frac{V_{th}}{R_2} \ln \left(1 + \frac{V_{CC} - 2v_{BE}}{V_A} \right)$$

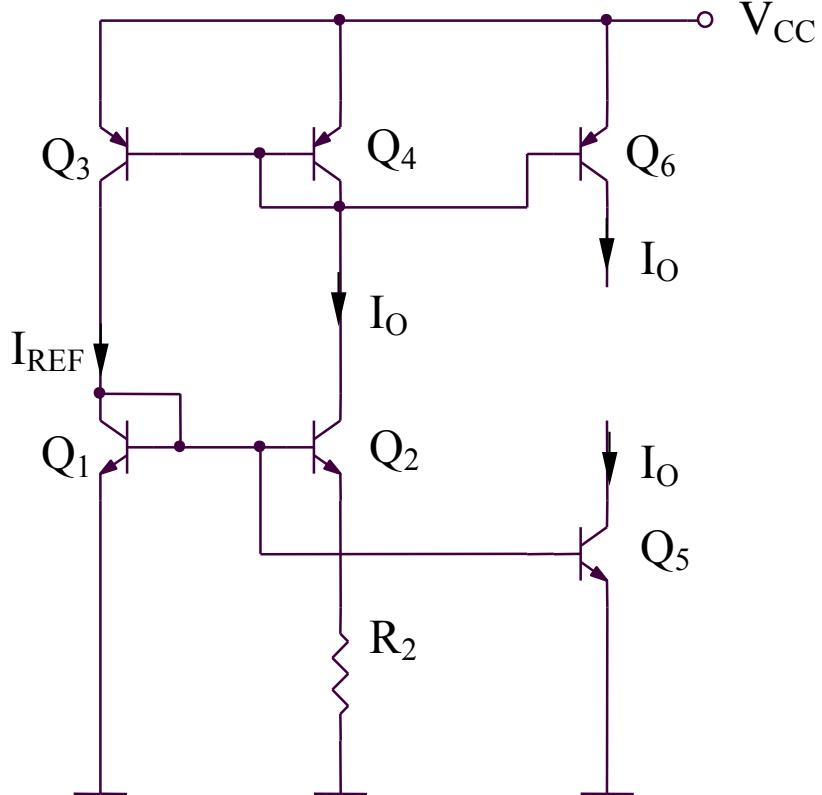
Derivand:

$$\frac{\partial I_O}{\partial V_{CC}} = \frac{V_{th}}{R_2(V_A + V_{CC})}$$

rezulta:

$$S_{V_{CC}}^{I_O} \cong \frac{V_{th}}{v_{BE}} \frac{1}{1 + \frac{V_A}{V_{CC}}}$$

Sursa de curent Widlar cu autopolarizare



$$I_O = \frac{v_{BE1} - v_{BE2}}{R_2}$$

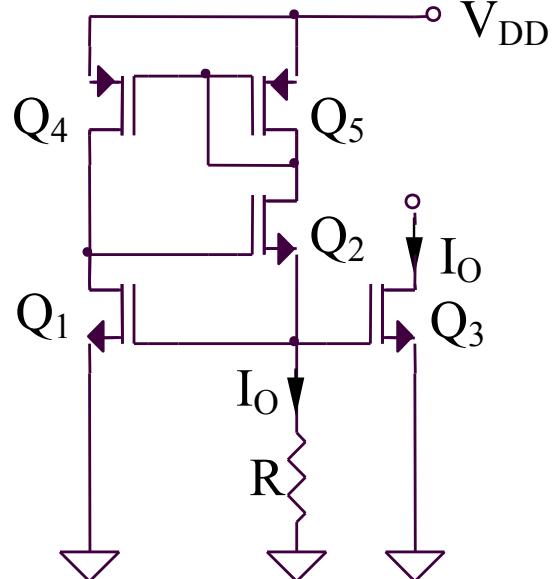
$$I_O = \frac{V_{th}}{R_2} \ln\left(\frac{I_{REF}}{I_O}\right) + \frac{V_{th}}{R_2} \ln\left(\frac{I_{S2}}{I_{S1}}\right)$$

$$I_O \cong \frac{V_{th}}{R_2} \ln\left(1 + \frac{V_{CC}}{V_A}\right) + \frac{V_{th}}{R_2} \ln\left(\frac{I_{S2}}{I_{S1}}\right)$$

$$S_{V_{CC}}^{I_O} \cong \frac{V_{CC}}{V_A} \frac{1}{\ln\left(\frac{I_{S2}}{I_{S1}}\right)}$$

Sursa de curent CMOS cu autopolarizare (1)

Curentul de ieșire



$$I_O = \frac{V_{GS}}{R} = \frac{K}{2} (V_{GS} - V_T)^2$$

$$\frac{KR}{2} V_{GS}^2 - (1 + KRV_T) V_{GS} + \frac{KR}{2} V_T^2 = 0$$

Rezolvând ecuația pentru V_{GS} rezulta:

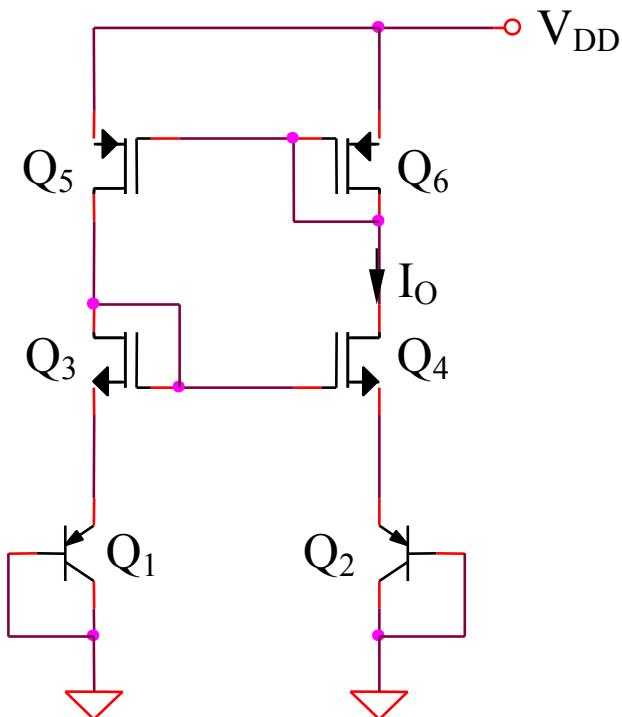
$$V_{GS1,2} = V_T + \frac{1}{KR} \pm \frac{\sqrt{2KRV_T + 1}}{KR}$$

$$V_{GS} = V_T + \frac{1}{KR} + \frac{\sqrt{2KRV_T + 1}}{KR}$$

Deci:

$$I_O = \frac{1}{KR^2} (1 + KRV_T + \sqrt{1 + 2KRV_T})$$

Sursa de curent CMOS cu autopolarizare (2)



Curentul de iesire

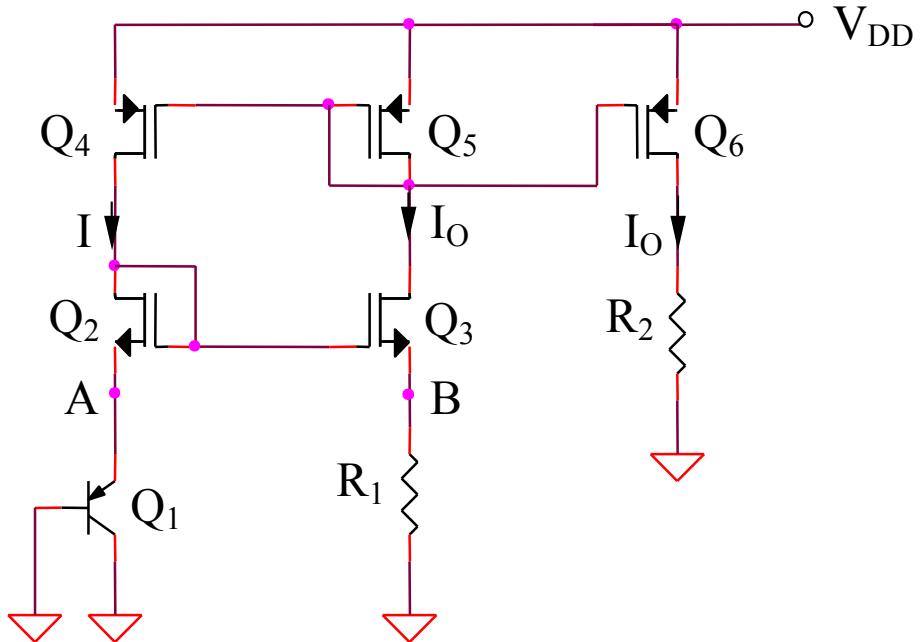
$$V_T + \sqrt{\frac{2I_O}{4K}} + V_{th} \ln\left(\frac{I_O}{I_S}\right) = \\ = V_T + \sqrt{\frac{2I_O}{K}} + V_{th} \ln\left(\frac{I_O}{10I_S}\right)$$

Rezulta:

$$I_O = 2K[V_{th} \ln(10)]^2$$

$$V_{th} = \frac{kT}{q} - \text{tensiunea termica}$$

Sursa de curent CMOS cu autopolarizare (3)



Curentul de ieșire

Pentru tranzistoare MOS identice,
 $V_A = V_B$, deci:

$$I_O = \frac{V_{EB1}}{R_1}$$

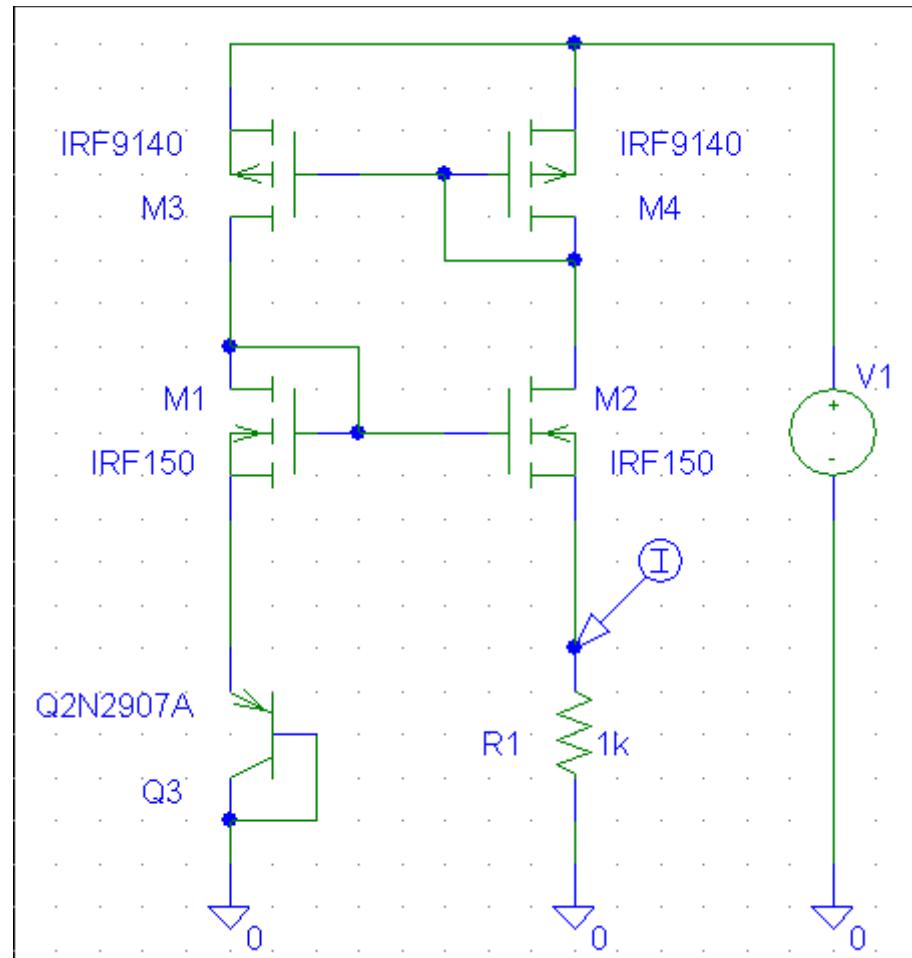
SIMULARI pentru sursa de curent CMOS cu autopolarizare (3)

Dependenta curentului de iesire de tensiunea de alimentare

SIMULARI pentru sursa de curent CMOS cu autopolarizare (3)

Dependenta curentului de iesire de tensiunea de alimentare

SIM 3.10: I_{D2} (V_1)



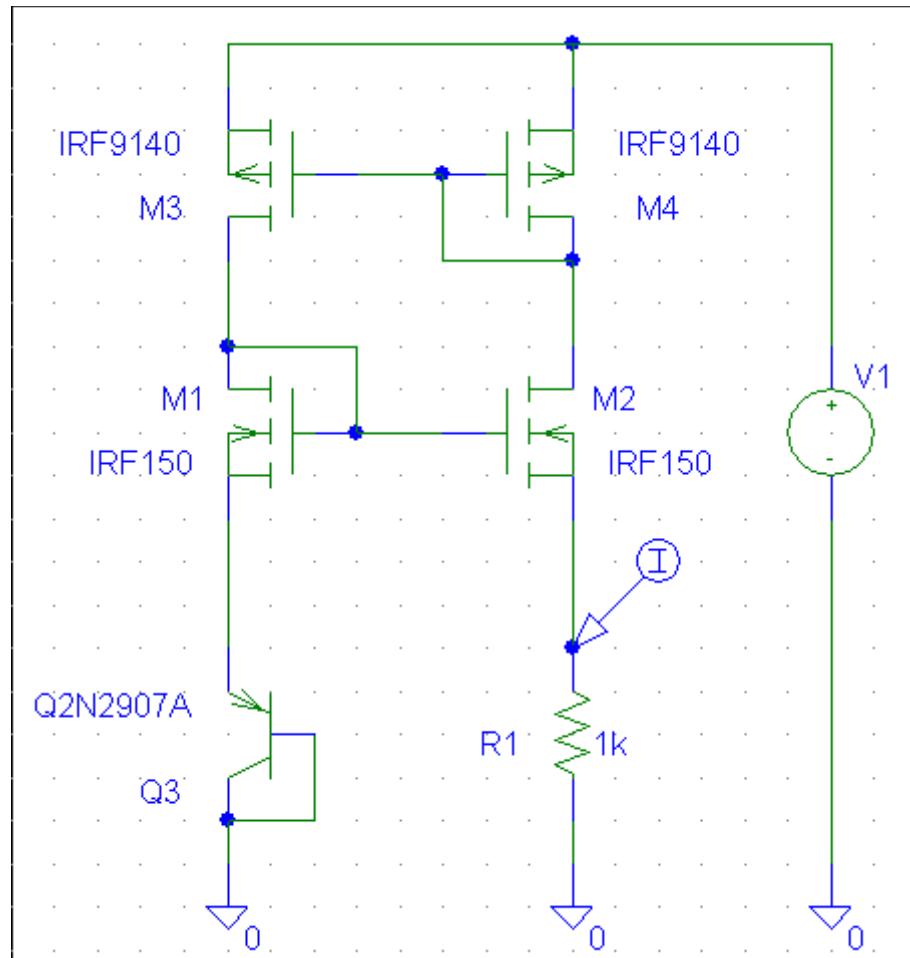
SIMULARI pentru sursa de curent CMOS cu autopolarizare (3)

Dependenta curentului de iesire de temperatura

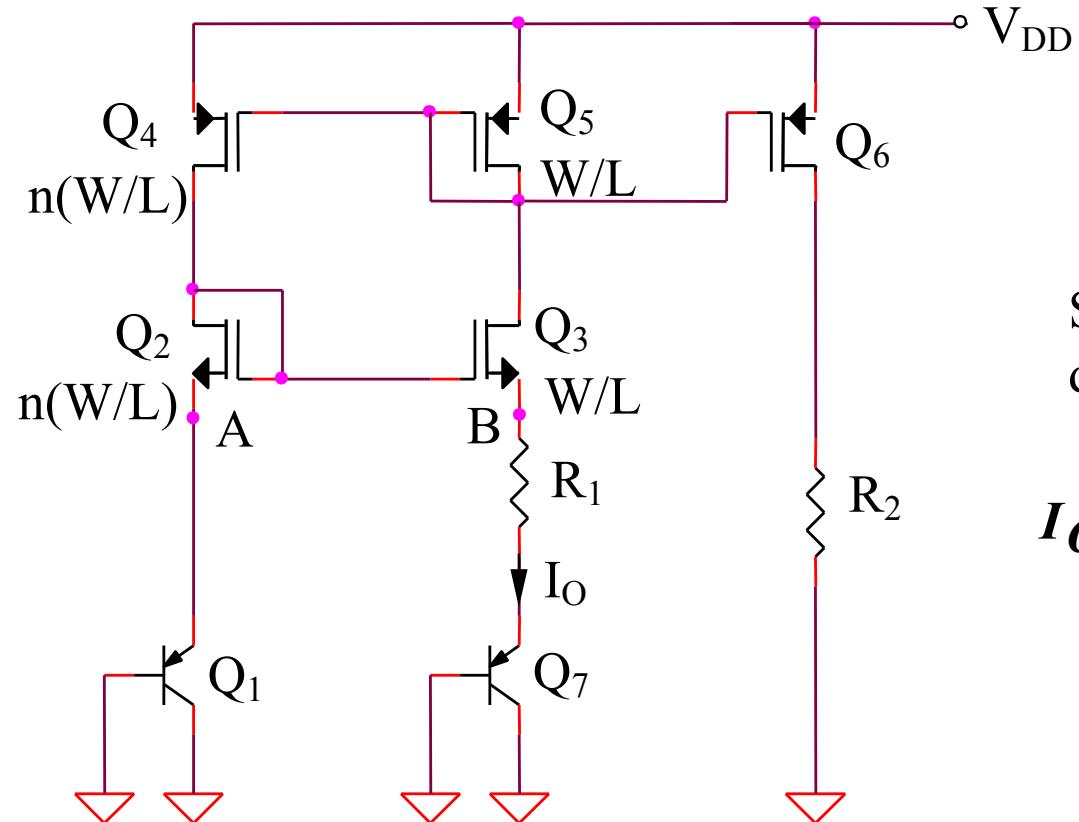
SIMULARI pentru sursa de curent CMOS cu autopolarizare (3)

Dependenta curentului de iesire de temperatura

SIM 3.11: $I_{D2}(t)$



Sursa de curent CMOS cu autopolarizare (4)

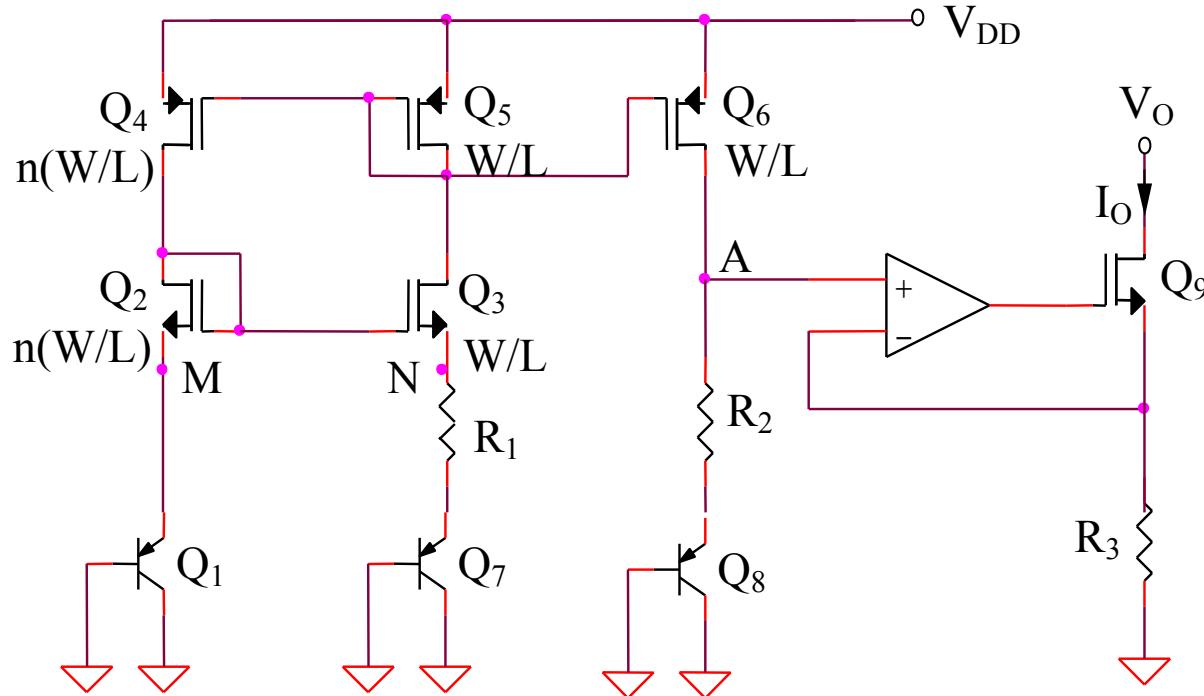


Curentul de ieșire

Se poate demonstra ca $V_A = V_B$,
deci:

$$I_O = \frac{|V_{BE1}| - |V_{BE7}|}{R_J} = \frac{V_{th}}{R_J} \ln(n)$$

Sursa de curent CMOS cu autopolarizare (5)

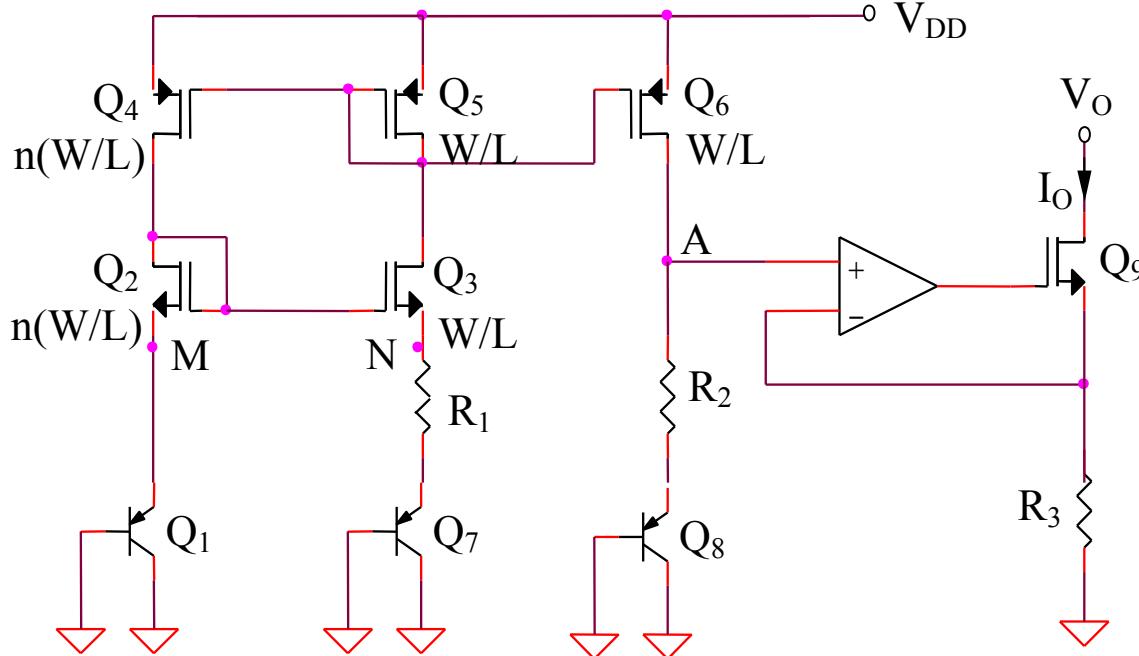


$$V_{GS2} = V_{GS3}$$

$$V_{R_2} = R_2 \frac{V_{EB1} - V_{EB7}}{R_1} = \frac{R_2}{R_1} V_{th} \ln(n) \quad \left. \right\} \Rightarrow I_O(T) = \frac{I}{R_3} \left[\frac{R_2}{R_1} V_{th} \ln(n) + V_{EB8}(T) \right]$$

$$V_{EB}(T) = A + BT + CT \ln\left(\frac{T}{T_0}\right)$$

Sursa de curent CMOS cu autopolarizare (5) – cont.



$$\Rightarrow I_O(T) = \frac{I}{R_3} \left[\frac{R_2 kT}{R_1 q} \ln(n) + A + BT + CT \ln\left(\frac{T}{T_0}\right) \right]$$

Conditia de corectie liniara a caracteristicii poate fi scrisa astfel:

$$B + \frac{R_2 k}{R_1 q} \ln(n) = 0$$

Rezulta:

$$I_O(T) = \frac{I}{R_3} \left[A + CT \ln\left(\frac{T}{T_0}\right) \right]$$

3.2. Surse de tensiune

3.2. Surse de tensiune

3.2.1. Clasificare

I. Surse de tensiune elementare

- complexitate redusa
- performante modeste

II. Surse de tensiune cu reactie

- rezistenta de iesire redusa
- complexitate medie

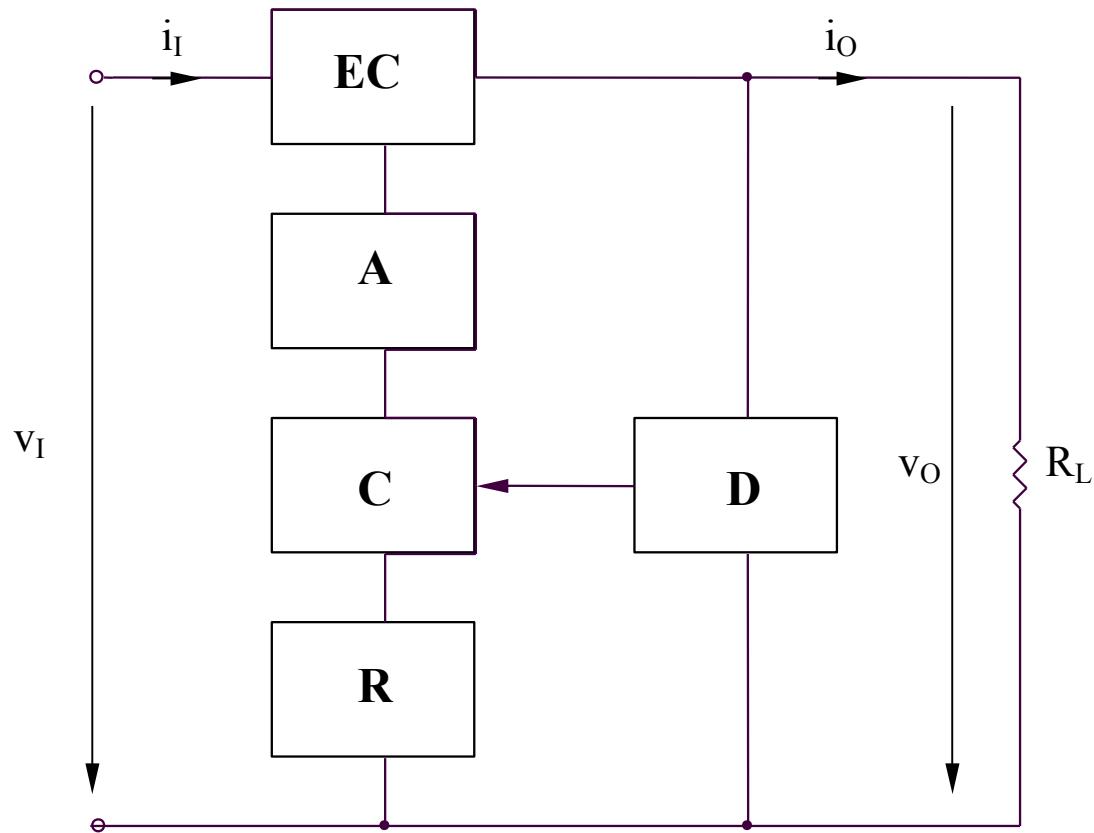
III. Surse de tensiune compensate cu temperatura

- dependenta redusa de temperatura a tensiunii de iesire
- complexitate ridicata

3.2.2. Surse de tensiune cu reactie

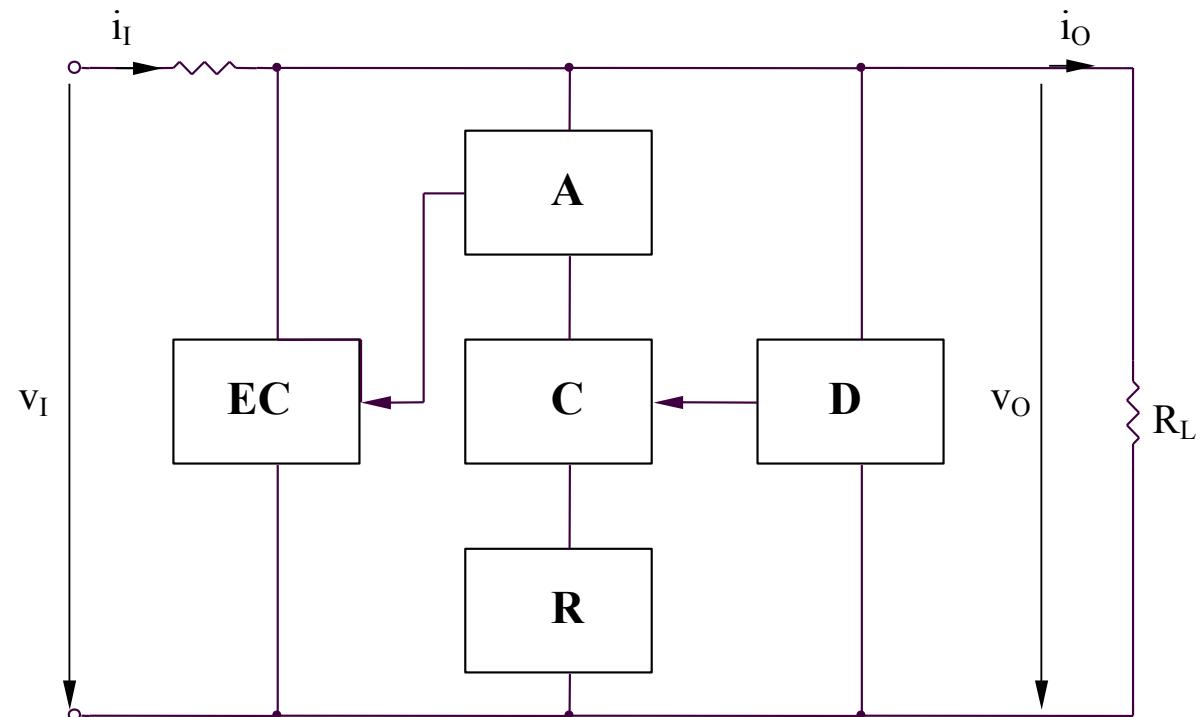
3.2.2. Surse de tensiune cu reactie

Surse de tensiune cu stabilizare serie (schema bloc)



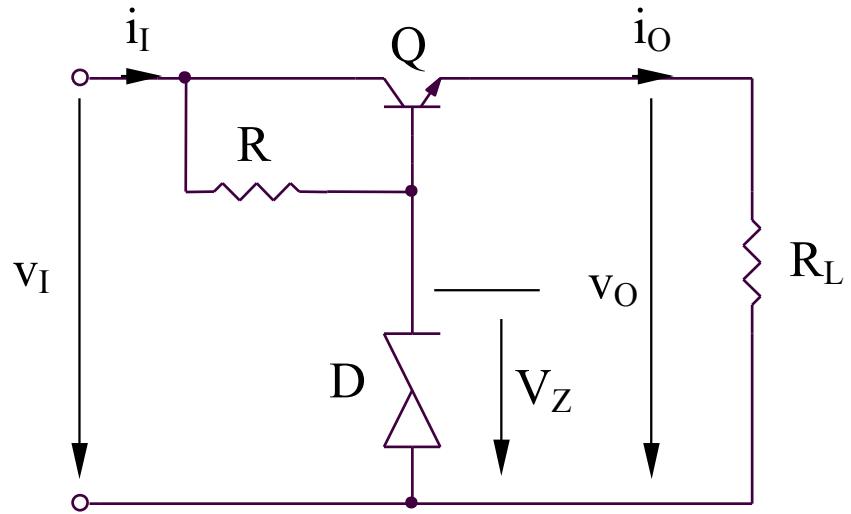
D = bloc de divizare
C = bloc de comparare
R = circuit de referinta
A = amplificator
EC = element de control

Surse de tensiune cu stabilizare paralel (schema bloc)

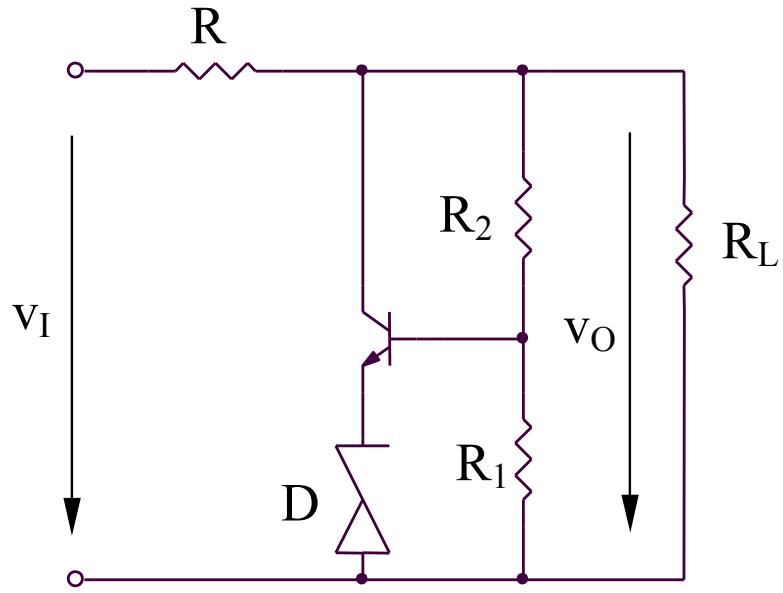


D = bloc de divizare
C = bloc de comparare
R = circuit de referinta
A = amplificator
EC = element de control

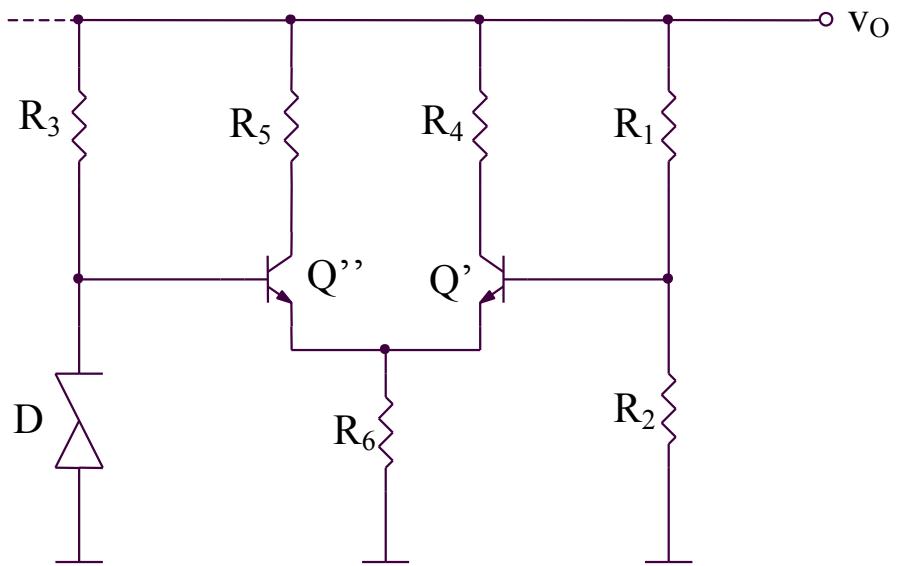
Exemplu de surse de tensiune



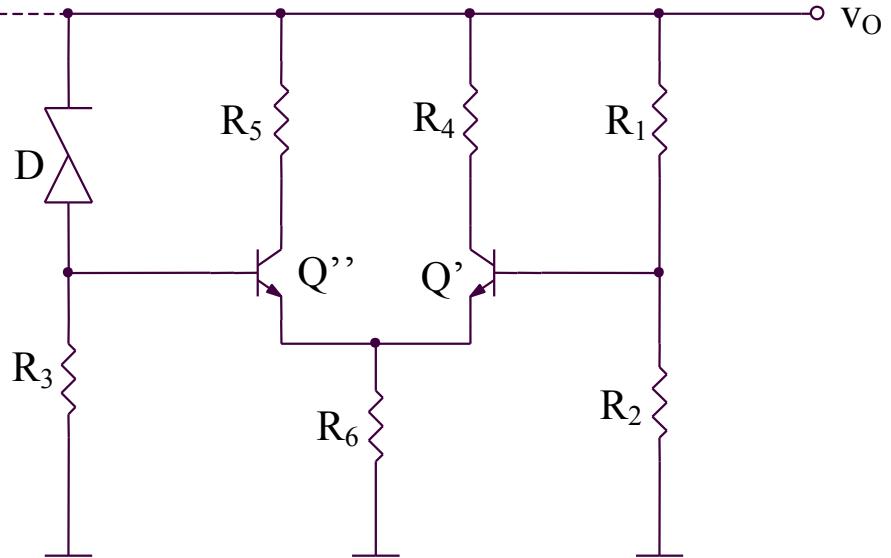
$$v_O = V_Z - V_{BE}$$



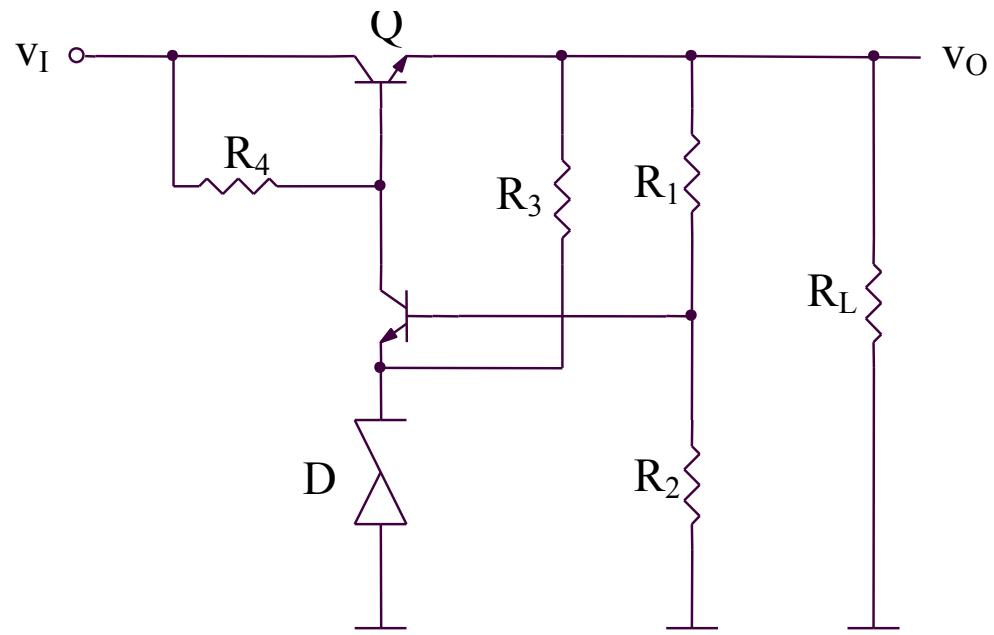
$$v_O = (V_{BE} + V_Z) \left(1 + \frac{R_2}{R_1} \right) > V_Z$$



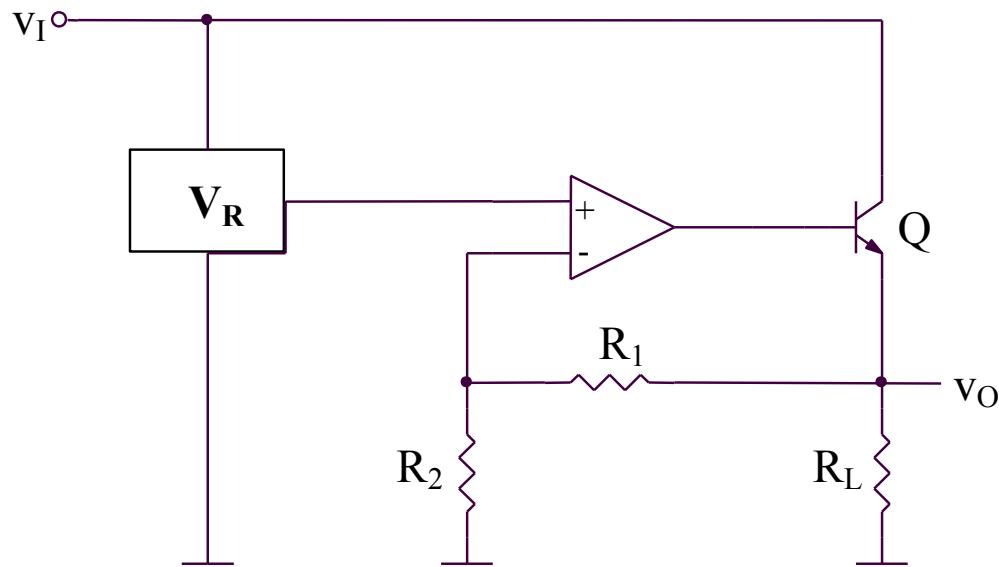
$$v_O = V_Z \left(1 + \frac{R_1}{R_2} \right)$$



$$v_O = V_Z \left(1 + \frac{R_2}{R_1} \right)$$

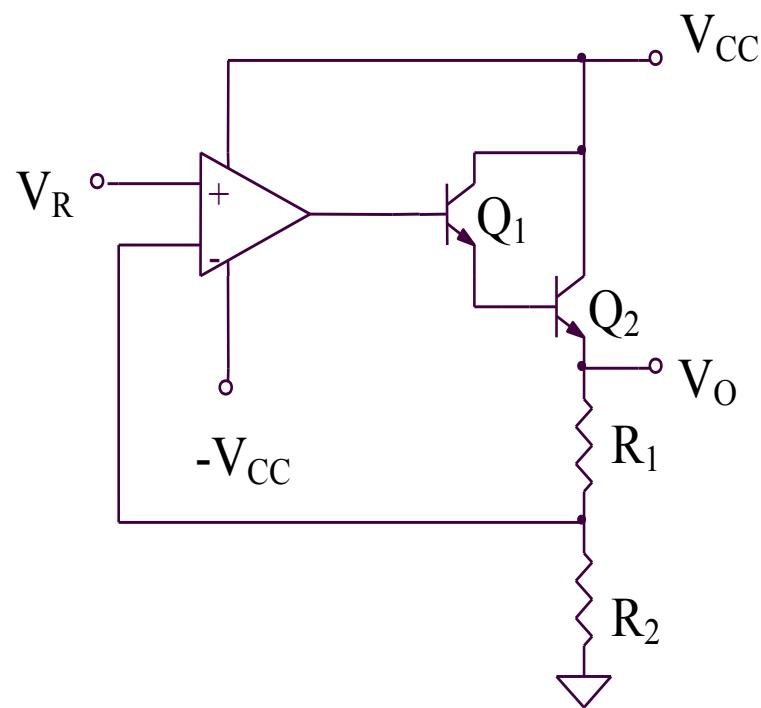


$$v_O = (V_Z + V_{BE}) \left(1 + \frac{R_1}{R_2} \right)$$



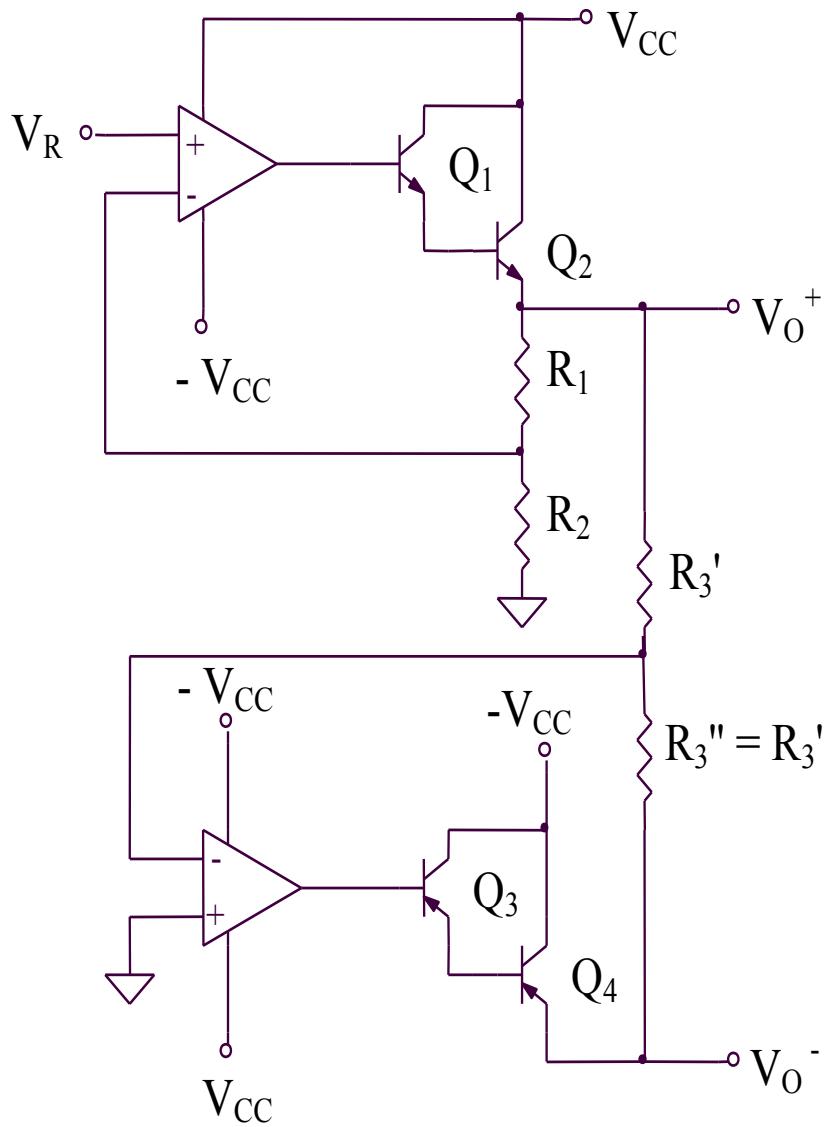
$$V_R = V_O \frac{R_2}{R_1 + R_2}$$

$$V_O = V_R \left(1 + \frac{R_1}{R_2} \right)$$



$$V_R = V_O \frac{R_2}{R_1 + R_2}$$

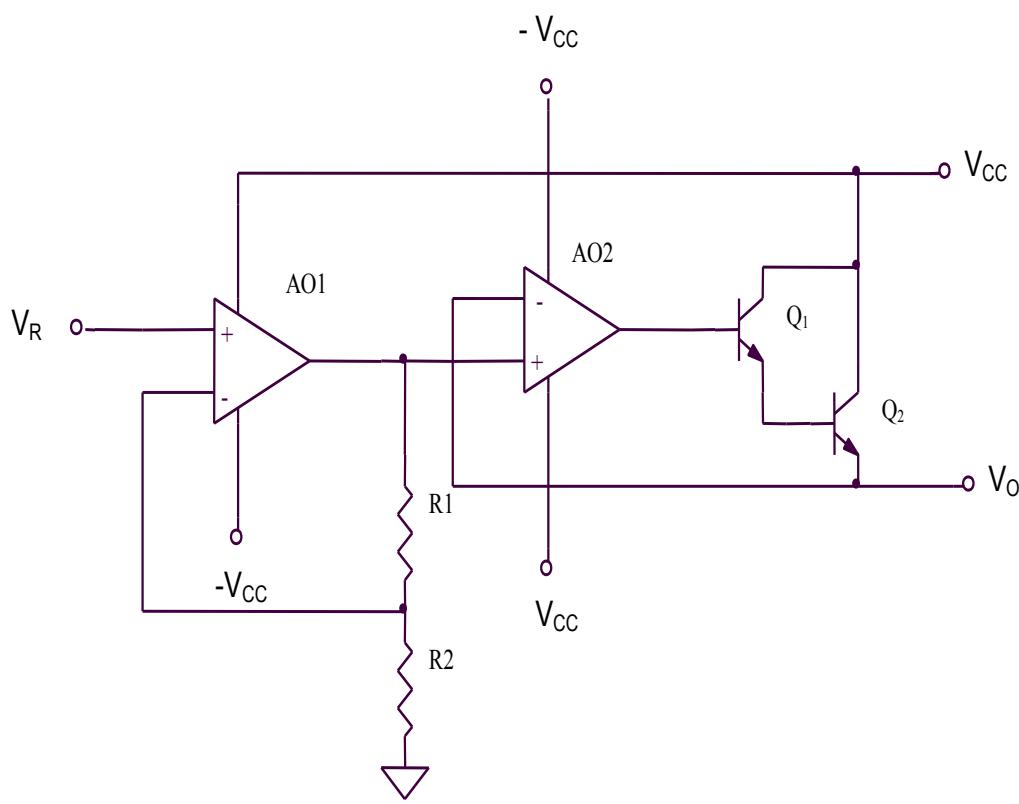
$$V_O = V_R \left(1 + \frac{R_1}{R_2} \right)$$



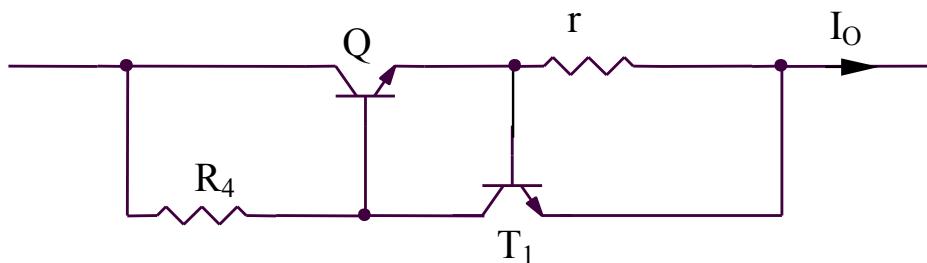
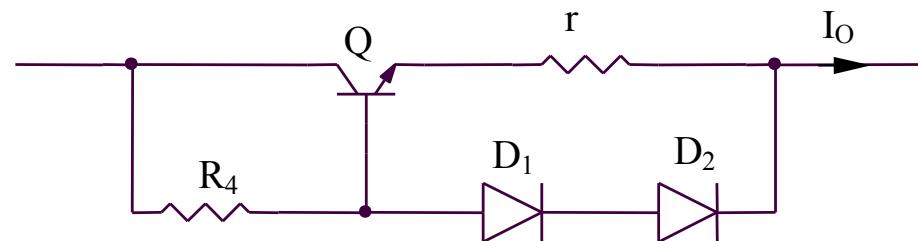
$$V_R = V_O^+ \frac{R_2}{R_1 + R_2}$$

$$V_O^+ = V_R \left(1 + \frac{R_1}{R_2} \right)$$

$$\frac{V_O^+}{R_3'} = -\frac{V_O^-}{R_3''} \Rightarrow V_O^- = -V_O^+$$



Protectia la suprasarcina (1)



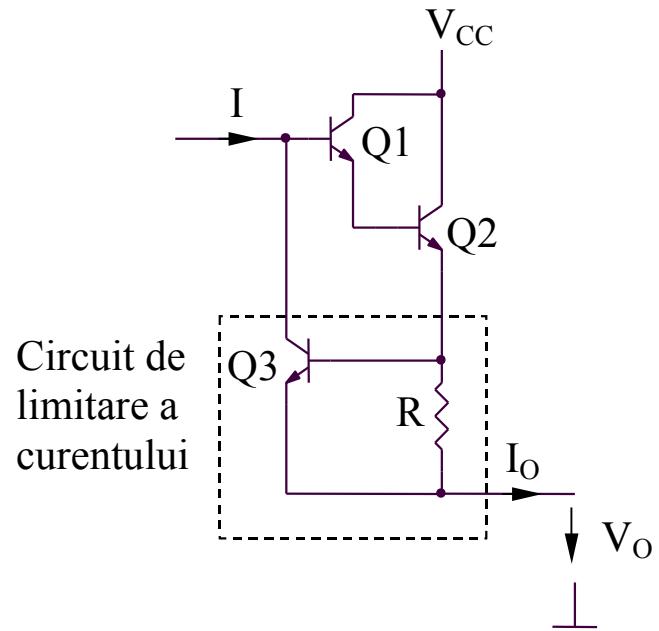
$$V_R = V_O \frac{R_2}{R_1 + R_2}$$

$$V_O = V_R \left(1 + \frac{R_1}{R_2} \right)$$

$$I_{OL} = \frac{V_{D1} + V_{D2} - V_{BE}}{r} \approx \frac{V_D}{r}$$

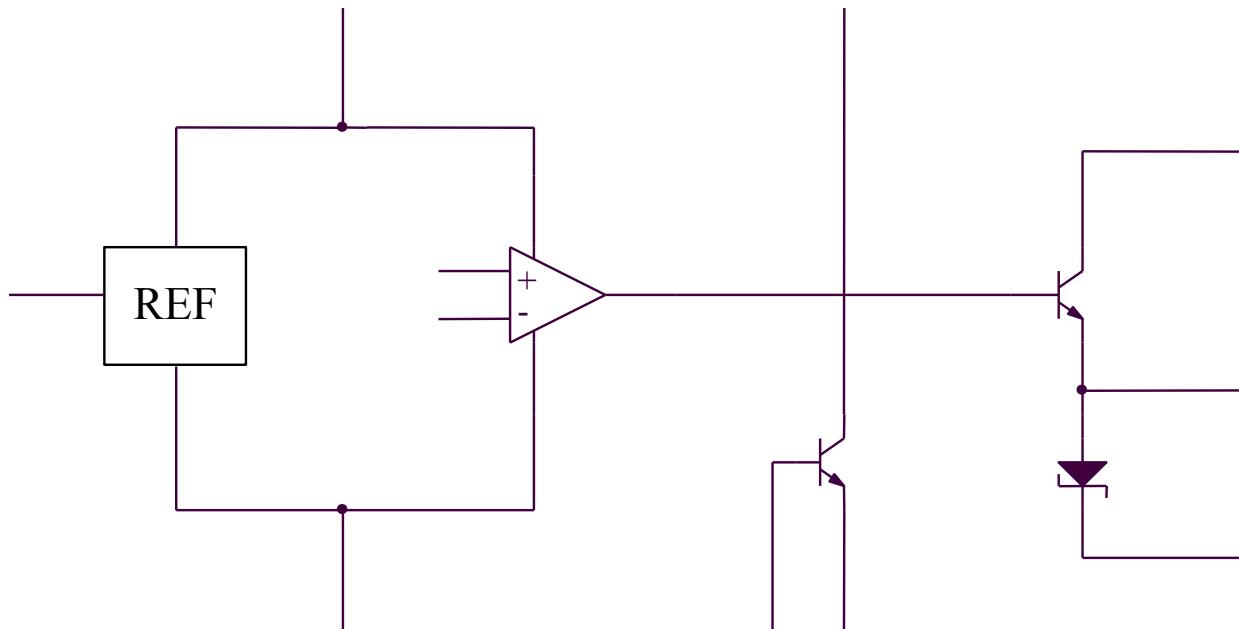
$$I_{OL} = \frac{V_{BE}}{r}$$

Protectia la suprasarcina (2)

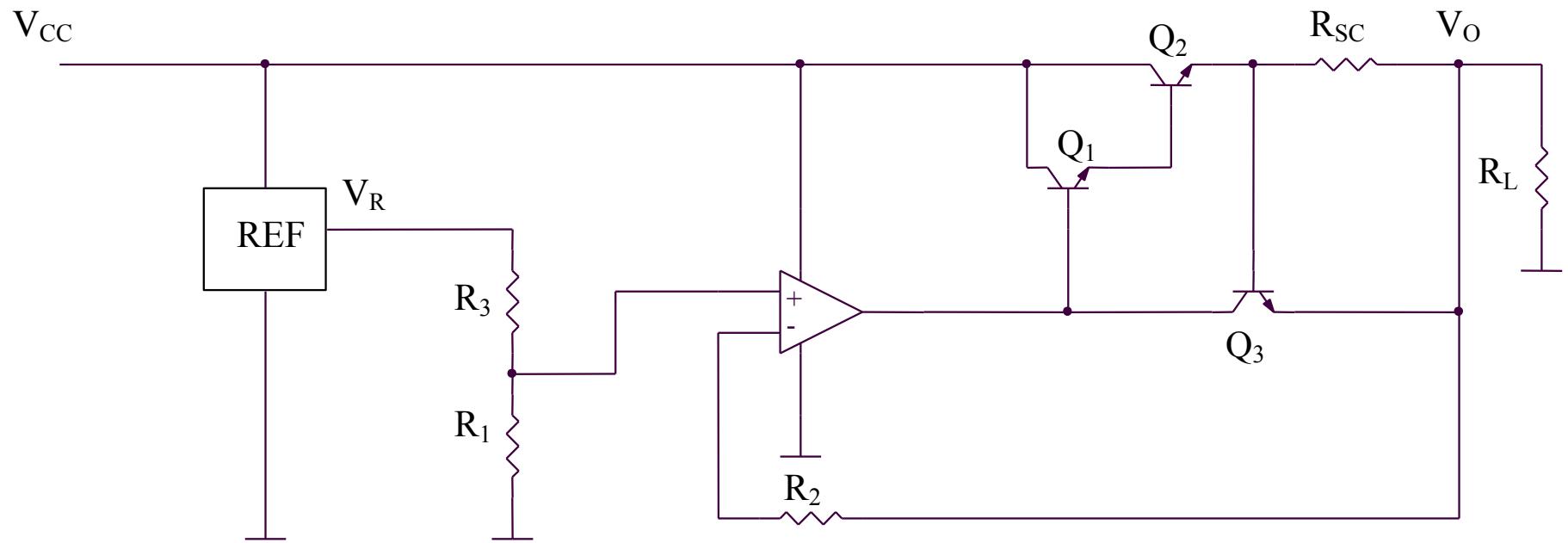


$$I_{OL} = \frac{V_{BE3}}{R}$$

circuitul BA 723



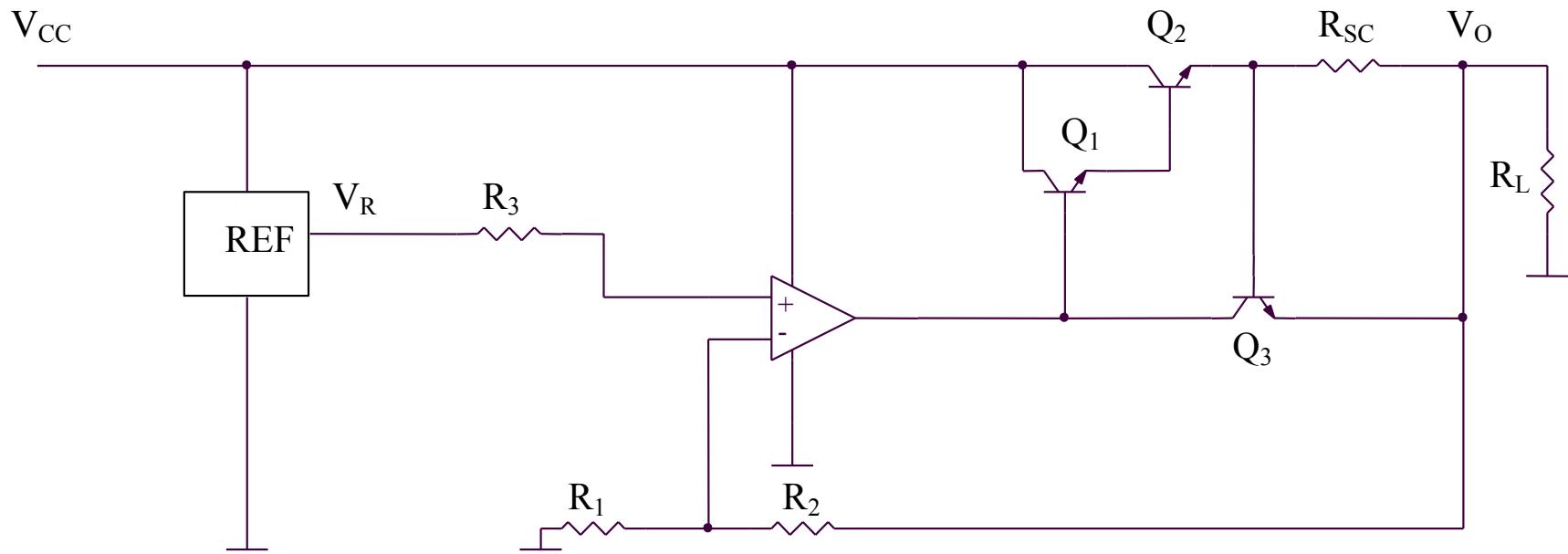
Sursa de tensiune pentru $V_O < V_R$



$$V_O = V_R \frac{R_1}{R_1 + R_3} < V_R$$

$$I_{Osc} = \frac{V_{BE}}{R_{sc}}$$

Sursa de tensiune pentru $V_O > V_R$



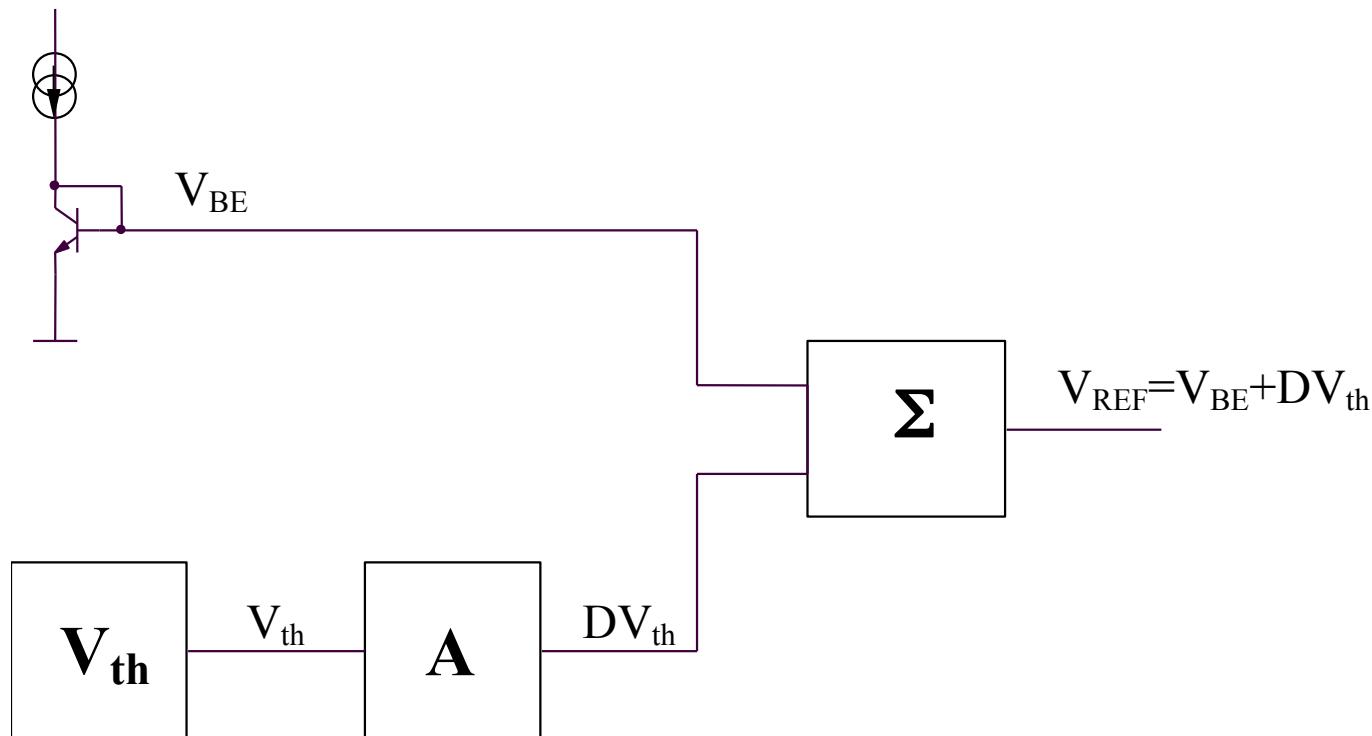
$$V_O \frac{R_1}{R_1 + R_2} = V_R \Rightarrow V_O = V_R \left(1 + \frac{R_2}{R_1} \right) > V_R$$

$$I_{Osc} = \frac{V_{BE}}{R_{sc}}$$

3.2.3. Surse de tensiune compensate cu temperatura

3.2.3. Surse de tensiune compensate cu temperatura

Referinte de tensiune bandgap (banda interzisa)



Dependenta de temperatura a tensiunii V_{BE}

$$\left. \begin{array}{l} V_{BE}(T) = V_{th} \ln \left[\frac{I_C(T)}{I_S(T)} \right] \\ I_S(T) = CT^\eta \exp \left(-\frac{E_{GO}}{V_{th}} \right) \end{array} \right\} \Rightarrow V_{BE}(T) = E_{GO} + \frac{kT}{q} \ln \left[\frac{I_C(T)}{CT^\eta} \right]$$

$$\left. \begin{array}{l} V_{BE}(T_O) = E_{GO} + \frac{kT_O}{q} \ln \left[\frac{I_C(T_O)}{CT_O^\eta} \right] \\ I_C(T) = BT^\alpha \end{array} \right\} \Rightarrow$$

$$\Rightarrow V_{BE}(T) = E_{GO} + \frac{V_{BE}(T_O) - E_{GO}}{T_O} T + (\alpha - \eta) \frac{KT}{q} \ln \left(\frac{T}{T_O} \right)$$

$$\frac{V_{BE}(T_O) - E_{GO}}{T_O} \cong -2,1 mV/K < 0$$

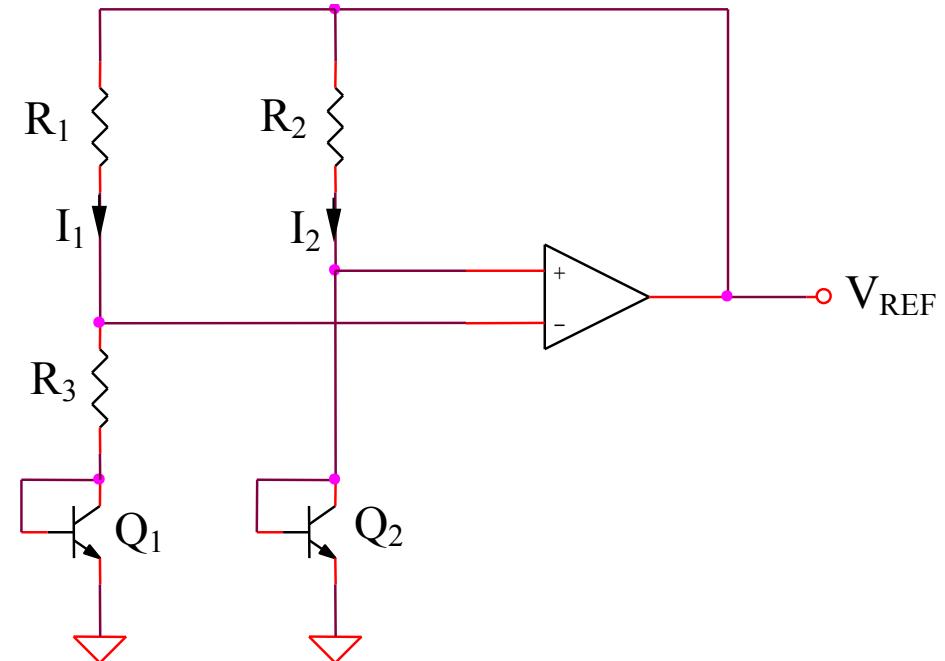
Functionarea referintelor de tensiune

$$\left. \begin{array}{l} V_{REF}(T) = DV_{th} + V_{BE}(T) \\ V_{BE}(T) = A + BT + CT \ln\left(\frac{T}{T_0}\right) \end{array} \right\} \Rightarrow$$

$$\Rightarrow V_{REF}(T) = A + \left(B + D \frac{k}{q} \right) T + CT \ln\left(\frac{T}{T_0}\right)$$

$$B + D \frac{k}{q} = 0 \Rightarrow V_{REF}(T) = A + CT \ln\left(\frac{T}{T_0}\right)$$

Referinta de tensiune (1)



$$I_1 = \frac{V_{BE2} - V_{BE1}}{R_3} = \frac{kT}{qR_3} \ln\left(\frac{I_2}{I_1}\right) \quad \Rightarrow$$

$$I_1 R_1 = I_2 R_2$$

$$\Rightarrow I_1 = \frac{kT}{qR_3} \ln\left(\frac{R_1}{R_2}\right)$$

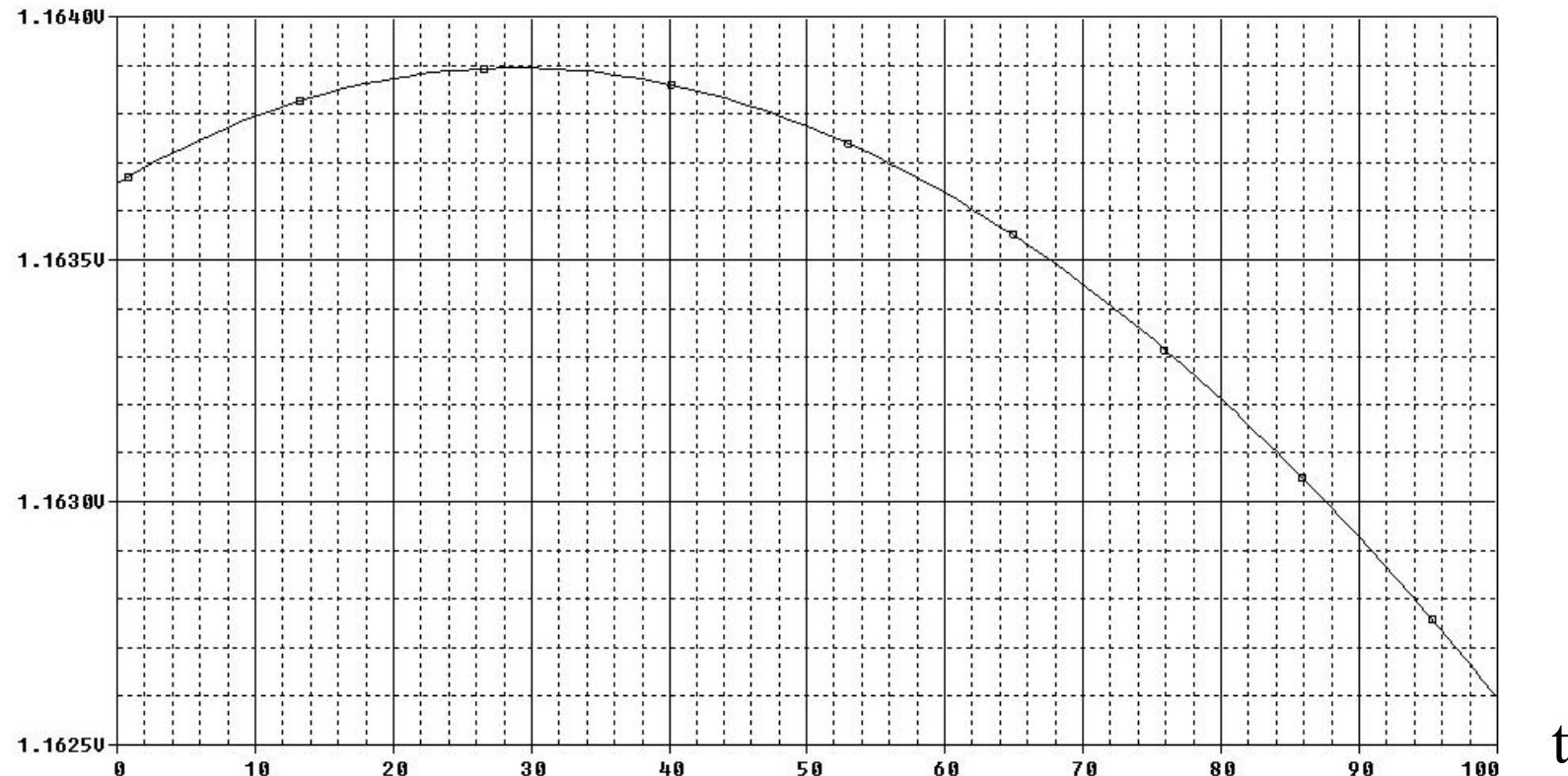
$$V_{REF}(T) = I_1(T)R_1 + V_{BE2}(T)$$

$$V_{BE}(T) = A + BT + CT \ln\left(\frac{T}{T_0}\right) \quad \Rightarrow$$

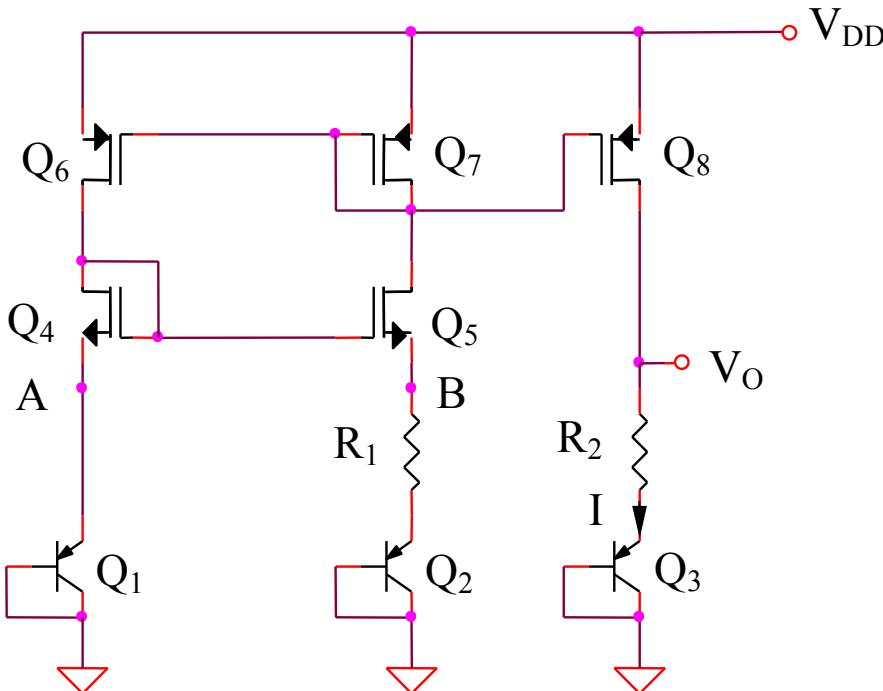
$$\Rightarrow V_{REF}(T) = A + \left[B + \frac{k}{q} \frac{R_1}{R_3} \ln\left(\frac{R_1}{R_2}\right) \right] T + CT \ln\left(\frac{T}{T_0}\right)$$

$$B + \frac{k}{q} \frac{R_1}{R_3} \ln\left(\frac{R_1}{R_2}\right) = 0 \Rightarrow V_{REF}(T) = A + CT \ln\left(\frac{T}{T_0}\right) \cong A \cong 1,2V$$

V_{REF}



Referinta de tensiune (2)



$$V_A - V_B = V_{GS5} - V_{GS4} = (V_{GS5} - V_T) - (V_{GS4} - V_T) = \sqrt{\frac{2I_{D5}}{K_5}} - \sqrt{\frac{2I_{D4}}{K_4}}$$

$$V_A - V_B = \sqrt{\frac{2I_{D5}}{K_5}} \left(1 - \sqrt{\frac{I_{D4}}{I_{D5}} \frac{K_5}{K_4}} \right) = \sqrt{\frac{2I_{D5}}{K_5}} \left(1 - \sqrt{\frac{I_{D6}}{I_{D7}} \frac{(W/L)_5}{(W/L)_4}} \right)$$

$$V_A - V_B = \sqrt{\frac{2I_{D5}}{K}} \left(1 - \sqrt{\frac{(W/L)_5}{(W/L)_4} \frac{(W/L)_6}{(W/L)_7}} \right)$$

Pentru: $\frac{(W/L)_4}{(W/L)_5} = \frac{(W/L)_6}{(W/L)_7} \Rightarrow V_A = V_B$

$$\Rightarrow V_O(T) = /V_{BE_3}(T)/ + I(T)R_2 = /V_{BE_3}(T)/ + \frac{/V_{BE_1}(T)/ - /V_{BE_2}(T)/}{R_1} R_2$$

$$V_O(T) = /V_{BE_3}(T)/ + \frac{R_2}{R_1} \frac{kT}{q} \ln \frac{I_{D6}}{I_{D7}}$$

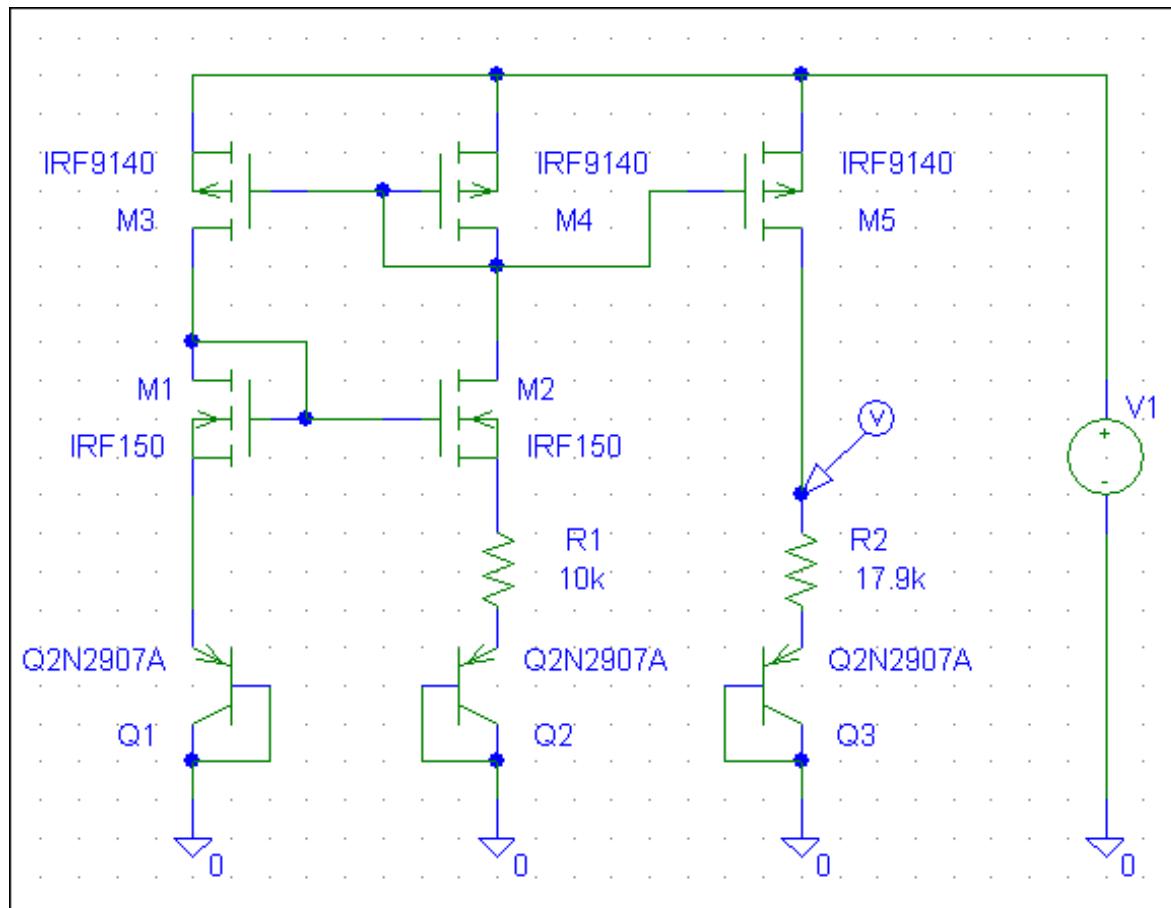
$$V_O(T) = /V_{BE_3}(T)/ + \frac{R_2}{R_1} \frac{kT}{q} \ln \left[\frac{(W/L)_6}{(W/L)_7} \right] \quad \left. \begin{array}{l} /V_{BE}(T)/ = A + BT + CT \ln \left(\frac{T}{T_0} \right) \\ B + \frac{R_2}{R_1} \frac{k}{q} \ln \left[\frac{(W/L)_6}{(W/L)_7} \right] = 0 \end{array} \right\} \Rightarrow V_O(T) = A + CT \ln \left(\frac{T}{T_0} \right)$$

SIMULARE pentru referinta de tensiune (2)
Dependenta de temperatura a tensiunii de referinta

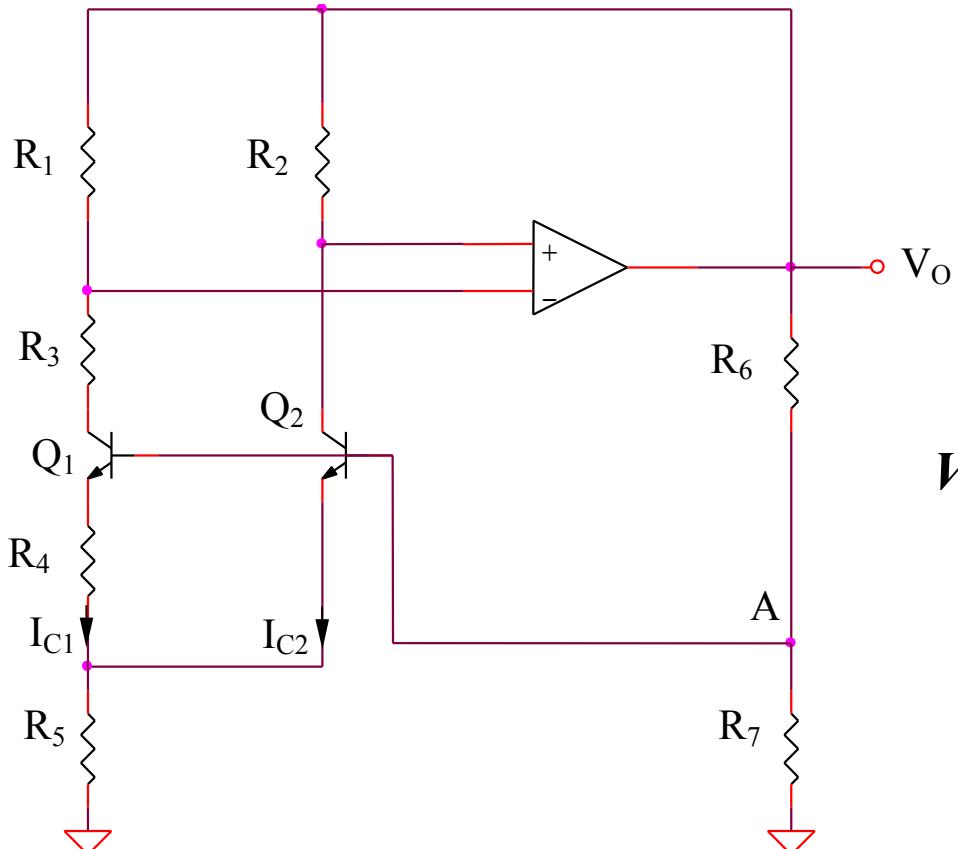
SIMULARE pentru referinta de tensiune (2)

Dependenta de temperatura a tensiunii de referinta

SIM 3.13: $V_{D5}(t)$



Referinta de tensiune (3)



$$\left. \begin{aligned} I_{C1} &= \frac{V_{BE2} - V_{BE1}}{R_4} = \frac{V_{th}}{R_4} \ln \frac{I_{C2}}{I_{C1}} \\ I_{C1} R_1 &= I_{C2} R_2 \end{aligned} \right\} \Rightarrow$$

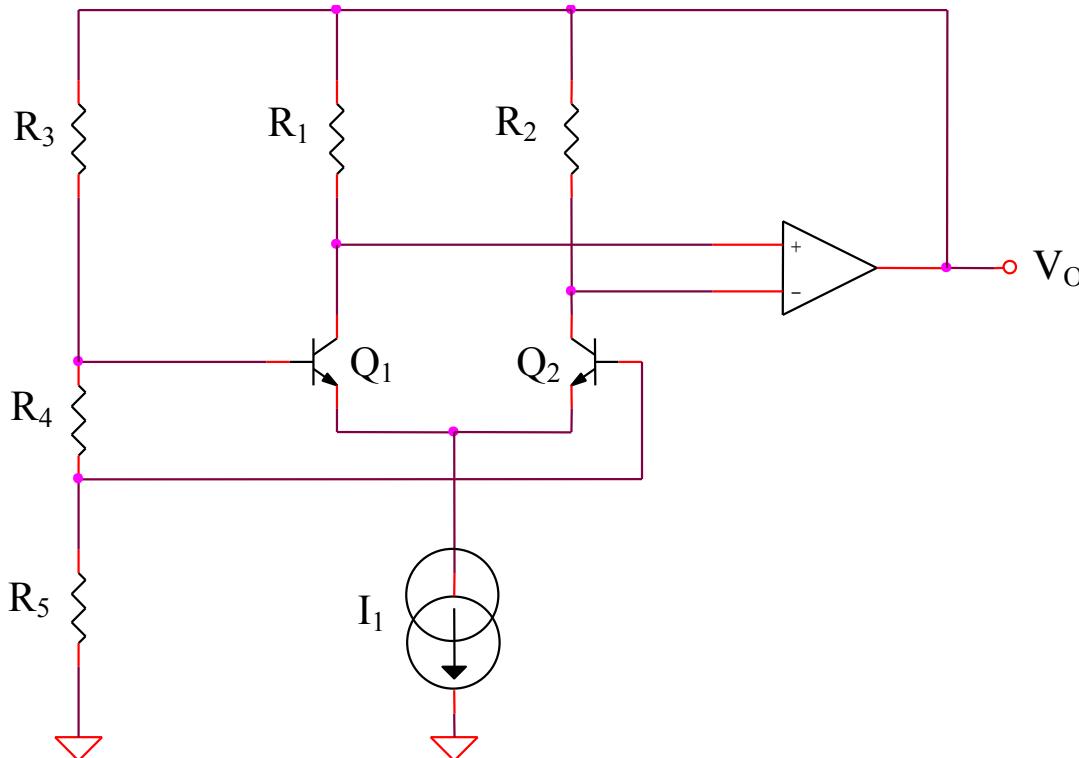
$$\Rightarrow I_{C1} = \frac{V_{th}}{R_4} \ln \frac{R_1}{R_2}$$

$$\left. \begin{aligned} V_A(T) &= (I_{C1} + I_{C2}) R_5 + V_{BE2}(T) \\ V_A(T) &= V_O(T) \frac{R_7}{R_6 + R_7} \end{aligned} \right\} \Rightarrow$$

$$\left. \begin{aligned} \Rightarrow V_O(T) &= \left(1 + \frac{R_6}{R_7} \right) \left[V_{BE2}(T) + \frac{R_5}{R_4} \left(1 + \frac{R_1}{R_2} \right) V_{th} \ln \left(\frac{R_1}{R_2} \right) \right] \\ &\quad \frac{R_5}{R_4} \left(1 + \frac{R_1}{R_2} \right) \frac{k}{q} \ln \left(\frac{R_1}{R_2} \right) + B = 0 \end{aligned} \right\} \Rightarrow V_O(T) = \left(1 + \frac{R_6}{R_7} \right) \left[A + CT \ln \left(\frac{T}{T_0} \right) \right]$$

Senzori de temperatura

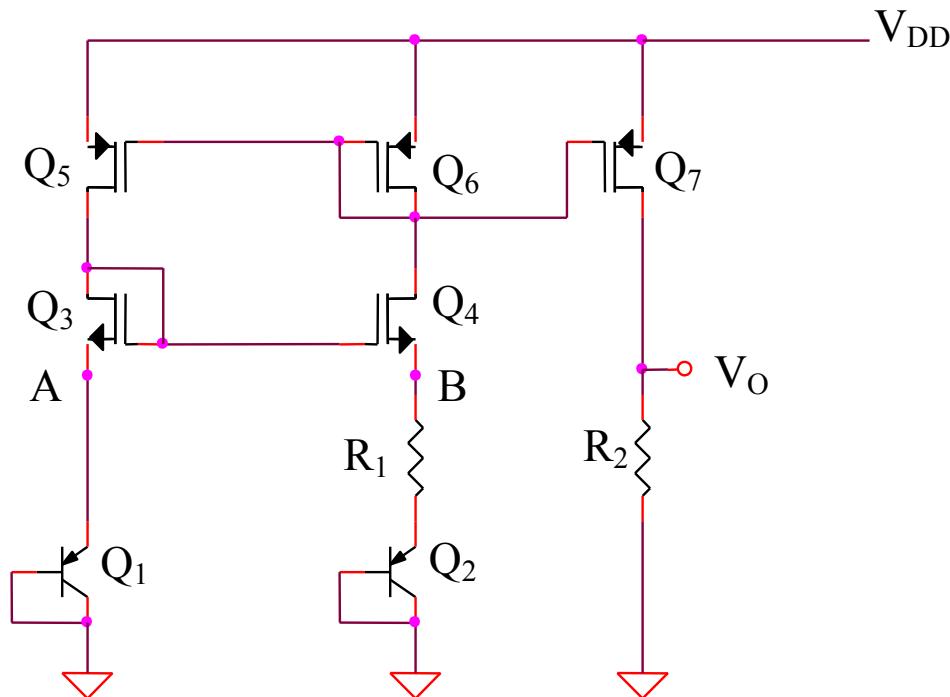
Exemplu (1)



$$V_O(T) \frac{R_4}{R_3 + R_4 + R_5} = V_{BE1} - V_{BE2} = V_{th} \ln \frac{I_{C1}}{I_{C2}} = V_{th} \ln \frac{R_2}{R_1} \Rightarrow$$

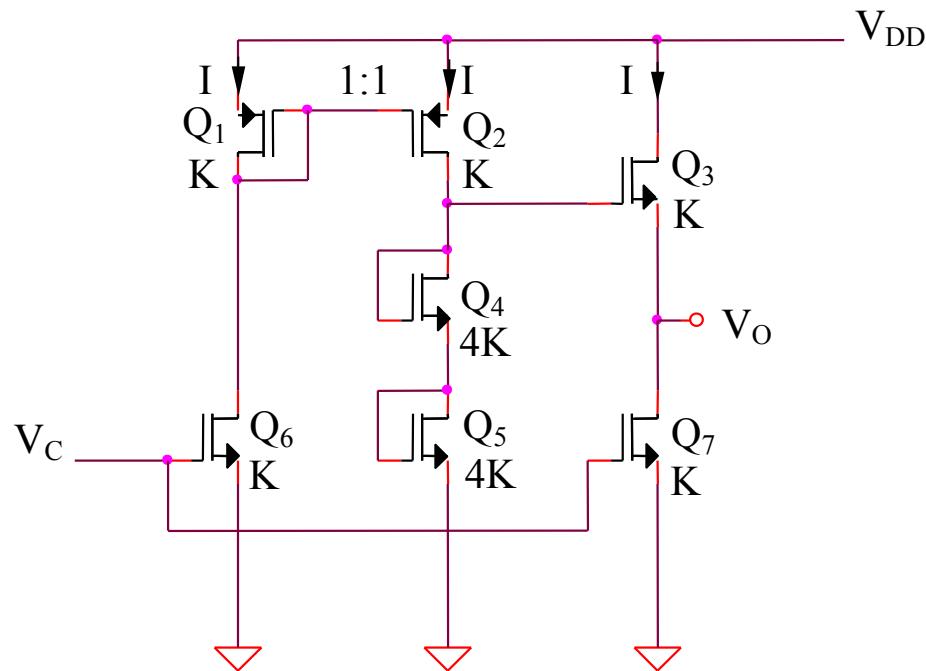
$$\Rightarrow V_O(T) = \left(1 + \frac{R_3 + R_5}{R_4} \right) V_{th} \ln \left(\frac{R_2}{R_1} \right) = ct \cdot T$$

Exemplu (2)



$$V_O = R_2 I_{D7}(T) = R_2 I_{D4}(T) = R_2 \frac{|V_{BE1}| - |V_{BE2}|}{R_1} = \frac{R_2}{R_1} V_{th} \ln \left[\frac{(W/L)_5}{(W/L)_6} \right] = ct \cdot T$$

Exemplu (3) – circuit de extragere a tensiunii de prag



$$V_O = 2V_{GS_4} - V_{GS_3} = 2\left(V_T + \sqrt{\frac{2I}{4K}}\right) - \left(V_T + \sqrt{\frac{2I}{K}}\right) = V_T = V_{T0} + a(T - T_0)$$